## 7.xi.

- 1. more about dynamic homology
- 2. search algorithms
- 3. traditional search strategies
- 4. new search strategies
- 5. tree form and consensus & compromise trees
- 6. summary

## Additional techniques using dynamic homology

AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTAGGCAACCCGGTAGGAT AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTAGGCAACCCTAGGATGC

Search-based optimization (SBO) improved/extended FSO

Iterative-pass optimization (IPO)

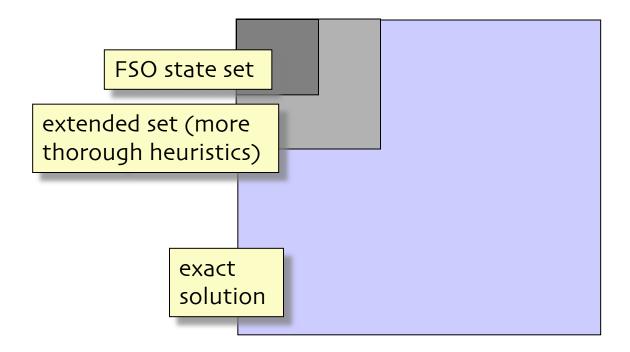
improved/extended DO

# Search-based optimization (SBO)

AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTAGGCAACCCGGTAGGAT AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTAGGCAACCCTAGGATGC

1) define the set of possible ancestal states

size of this set can vary



# Search-based optimization (SBO)

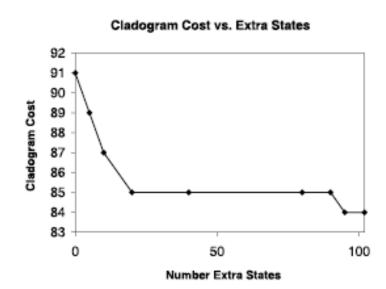
AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTAGGCAACCCGGTAGGAT AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTAGGCAACCCTAGGATGC

1) define the set of possible ancestal states

size of this set can vary

2) evaluate this set on a given tree

compared to FSO also OTHER sequences than those of the terminals will be used



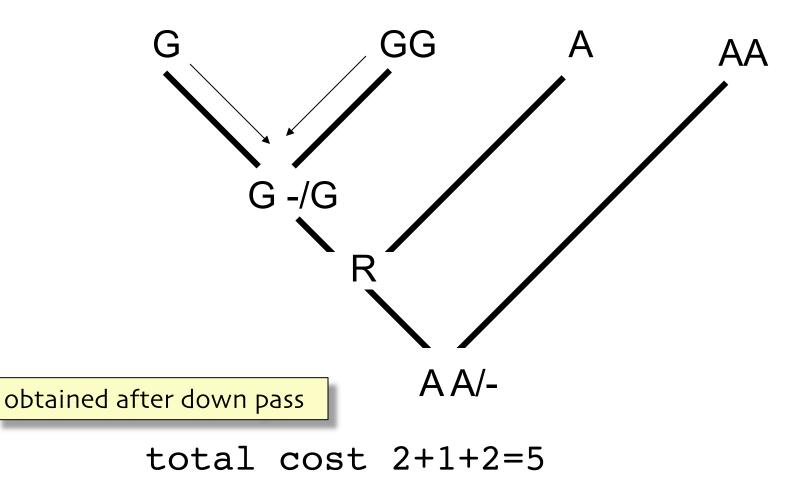
leads to CONSIDERABLE reduction of tree length

# Iterative pass optimization (IPO)

AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTA WHY ? GATGO

# Direct optimization (DO)

AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTAGGCAACCCGGTAGGAT



# Iterative pass optimization (IPO)

AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTAGGCAACCCGGTAGGAT

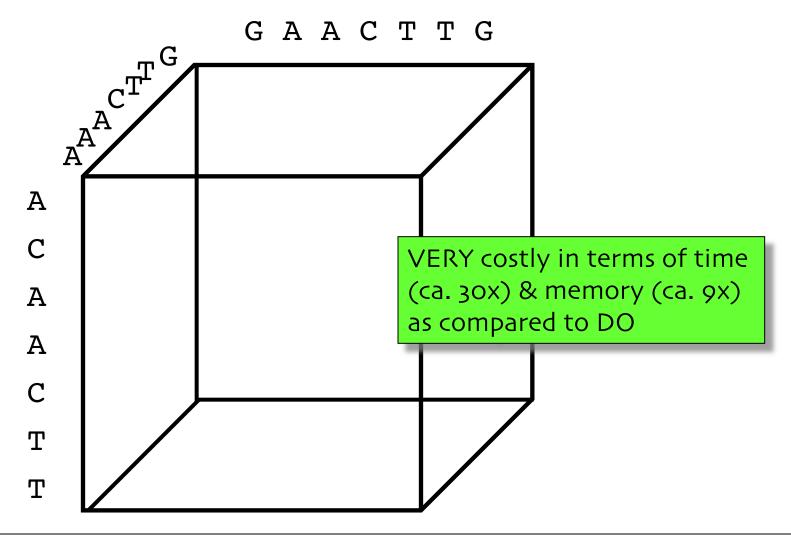
1) initiation: sequences for HTU's obtained e.g with down-pass of DO

2) up-pass is run iteratively, reevaluating each internal node with its 2 descendants & parental node SIMULTANEOUSLY 3 dimensional N-W algorithm each internal node is connected to 3 other nodes, if 1 is changed also 2 others have to be reevaluated

this is done until solutions stabilize

when initiated with DO normally 3 iterative passes needed

3) cost calculation of the final tree (taking into account int. node sequences inferred using IPO) compared to DO leads to reduction of tree length



3 sequences with 4 nucleotides --->  $4 \times 4 \times 4$  cells in a matrix =  $4^3$ Size of the matrix N<sup>M</sup> (N sequence length, M number of sequences)

# Dynamic homology analyses in practice

AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTAGGCAACCCGGTAGGAT AACGGTTTAAGGTACGGAGAATTAGGCAACCCTAGGATGCGATGCGCAGAGTTAGGTACGGAGAATTAGGCAACCCTAGGATGC

1) CLUSTAL (or other similarily fast) alignment

2) conserved regions easily found

3) sequences cut into fragments using e.g. winclada

should be performed cautiously, only WITHIN conserved

regions can lead to HUGE speed-up of analyses

analyses of only small materials possible using computers with only 1 CPU

parallelization leads to LARGE speed-up of analyses



Cladistics (2015) 1-9

10.1111/cla.12142

Cladistics

## Comparison of heuristic approaches to the generalized tree alignment problem

Eric Ford<sup>a,b,\*</sup> and Ward C. Wheeler<sup>b</sup>

<sup>a</sup>Department of Mathematics & Computer Science, Lehman College, CUNY, Bronx, NY 10468, USA; <sup>b</sup>Division of Invertebrate Zoology, American Museum of Natural History, New York, NY 10024, USA

Accepted 10 September 2015

#### Abstract

netic

Two commonly used heuristic approaches to the generalized tree alignment problem are compared in the context of phyloge-

MSA MSA+TS implementations and DO were compared... in addaese impart of all cases examined, DO outperformed MSA+TS with average improvement in parsimony score of ca. 15%

A central goal of biological systematics is mapping the relationships among organisms and groups of organisms—both extant and extinct—based on the reconstruction of phylogenetic trees using comparative character data. The generalized tree alignment problem (GTAP; Sankoff, 1975) is defined as the search for phylogenetic tree(s)—and associated vertex (hypothetical ancestor) sequences—with lowest cost for those data under maximum parsimony.

There has been an ongoing debate in the literature regarding multiple sequence alignment (Katoh et al., 2002; Edgar, 2004; Wheeler, 2007), with several aligners available. In addition, much effort has been expended to improving search on aligned sequences (Goloboff et al., 2003). At the same time, other paradigmata for approaching the GTAP are also available, chief among those being direct optimization (DO) (Wheeler, 1996, 2003; Varón and Wheeler, 2012, 2013). It has been the experience of many investigators that DO gives significantly better results than the two-step process of alignment followed by search for both real and simulated

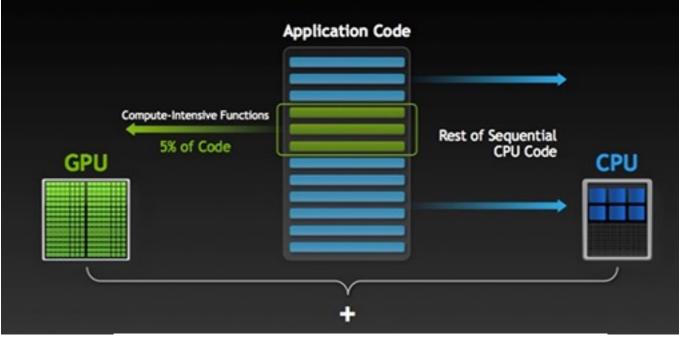
data (e.g. Lindgren and Daly, 2007; Lehtonen, 2008 Liu et al., 2009; Giribet and Edgecombe, 2013). In addition, the high degree of complexity in the settings of the software tools used for alignment and search only confuses the matter, as default settings are often used, and these defaults do not necessarily correspond between aligner and search engine. Here, we compare DO with two-step solutions directly. We also test whether the results of searches where alignment and search setting correspond are better (i.e. more optimal) than those in which they do not. We find that DO results in the discovery of shorter trees, by an average factor of 15%. In addition, using the two-step approach we found significantly (approximately 4%) shorter trees when using settings on alignment that match the settings of subsequent tree search (as opposed to the default settings of multiple sequence alignment (MSA) implementations).

### Software tools

We ran comparisons using several pieces of alignment software. What follows is a brief description of each package.

\*Corresponding author: E-mail address: eford@gradcenter.cuny.edu

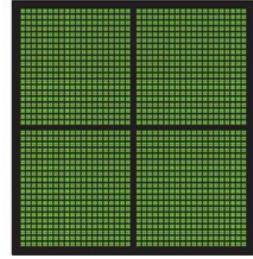
## **How GPU Acceleration Works**



nvidia.com/object/what-is-gpu-computing.html



CPU MULTIPLE CORES



GPU THOUSANDS OF CORES

### haskell.org

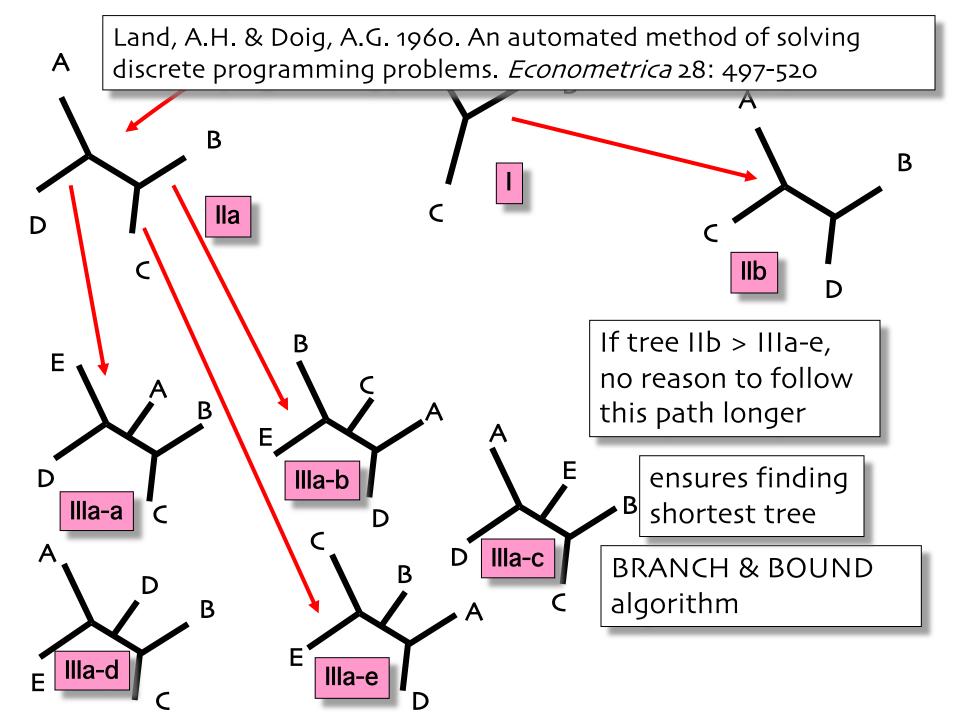
## https://github.com/amnh/PCG

♥ Why GitHub? ✓ Team Enterprise	e Explore $\vee$ Marketplace Pricing $\vee$	Search / Sign in Sign up
amnh / PCG Public		ب Notifications & Fork 1 ب کل Star 18 ب
<> Code 🕑 Issues 43 ুণ্ট Pull requests	🕑 Actions 🗄 Projects 🖽 Wiki 🕛 Security 🗠 Insights	
ੀ master 🗸 ੀ 8 branches 🛇 4 tag	Go to file	Code - About
Boarders Temporarily remove static lir	nking 002a04c on Dec 1, 2021 🕚 5,00	Phylogenetic Component Graph
.github/workflows		months ago haskell bioinformatics
арр	Cleaning up project root directory 9 r	months ago graph-algorithms phylogenetics
bench 📃	Updating documentation for completness 10 r	months ago comparative-genomics
🖿 bin	docs: Updating documentation.	3 years ago
config	Cleaning up project root directory 9 r	nonths ago
doc	Merge branch 'master' of https://github.com/amnh/PCG 9 r	nonths ago
lib	Updating documentation for completness 10 r	☆ 18 stars
prototype		nonths ago If ork
test	Updating documentation for completness 10 r	nonths ago
🗅 .gitignore	Updating intgration tests to check for an input error and parse error.	3 years ago Releases
🗅 README.md	Cleaning up project root directory 9 r	months ago 🛛 🛇 4 tags
🗅 cabal.project	Managing pinned dependencies; adding GHC-9.0.1 to build matrix 11 r	nonths ago
🗋 makefile	Ensuring a modern version of weeder 6 r	nonths ago Packages

## В

3	<b>1</b> exha
4	<b>3</b> poss
5	15
6	105
7	945
8	10 395
9	135 135
10	2 X 10 <sup>6</sup>
1 -	8 x 10 <sup>12</sup>
15	
20	<b>2</b> X 10 <sup>20</sup>
50	3 X 10 <sup>74</sup>

exhaustive search possible for only VERY limited no. of terminals



### \_\_\_\_\_

Т

B(T)

5
<b>O5</b> BRANCH and BOUND
945 algorithm
<b>O 395</b>   can be used for max. ca. 30 terminals
35 135
X 10 <sup>6</sup>
45
3 X 10 <sup>12</sup>
X 10 <sup>20</sup>
X 10 <sup>74</sup>

# HEURISTIC SEARCH

## Wagner algorithm

Kluge, A. G. & Farris, J. S. 1969. Quantitative phyletics and the evolution of anurans. *Systematic Zoology* 18:1-32.

Farris, J. S. 1970. Methods for computing Wagner trees. *Systematic Zoology* 19:83-92.



# **Basics of Cladistic**

### WAGNER TREES

A second way to construct a cladogram is to connect taxa together one at a time until all the taxa have been added. When added, each taxon is joined to the tree to minimize the number of character state changes.

Consider again the small data set:

	Characters				
	1	2	3	4	5
Outgroup	0	0	0	0	0
A	1	0	0	0	0
в	1	1	0	1	0
С	1	0	1	1	1

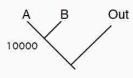
1. Find the organism with the lowest number of derived character states and connect it to the outgroup.

		Cl	hara	cter	5	#advanced	steps
	1	2	3	4	5		
Outgroup	0	0	0	0	0	0	
A	1	0	0	0	0	1	
в	1	1	0	1	0	3	
С	1	0	1	1	1	4	

Organism A has the lowest number of advanced steps:



2. Now find the organism with the next lowest number of derived character states. Write its name beside the first organisms' name and connect it to the line that joins the outgroup and the first organism. At the point where the two lines intersect, list the most advanced state present in both of the two organisms. For the above character set, the second organism is B:



Diana Lipscomb George Washington University Washington D.C. Copywrite (c) 1998

рр. 13-18

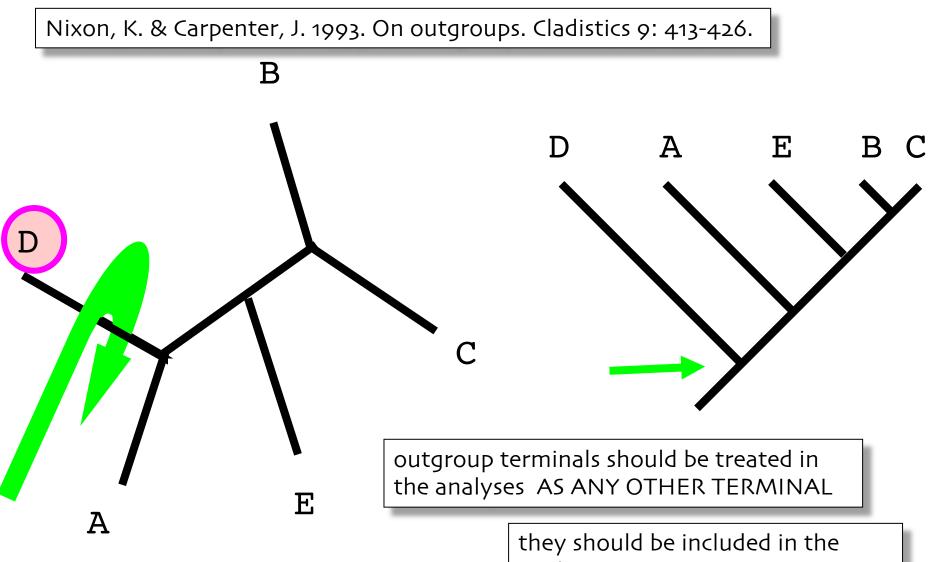
© 1998, D. Lipscomb

# Wagner algorithm

page 13:

1. Find the organism with the lowest number of derived character states and connect it to the outgroup

in practice ANY of the organisms can be used as outgroup



analyses FROM THE VERY START

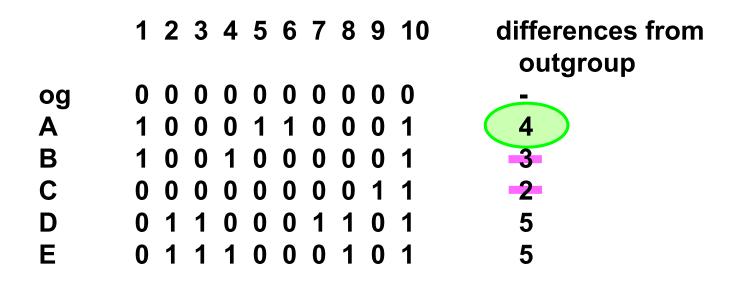
# Wagner algorithm

page 13:

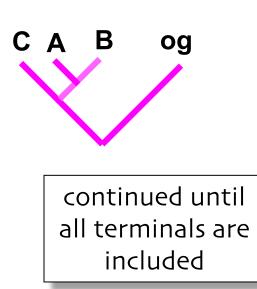
1. Find the organism with the lowest number of derived character states and connect it to the outgroup

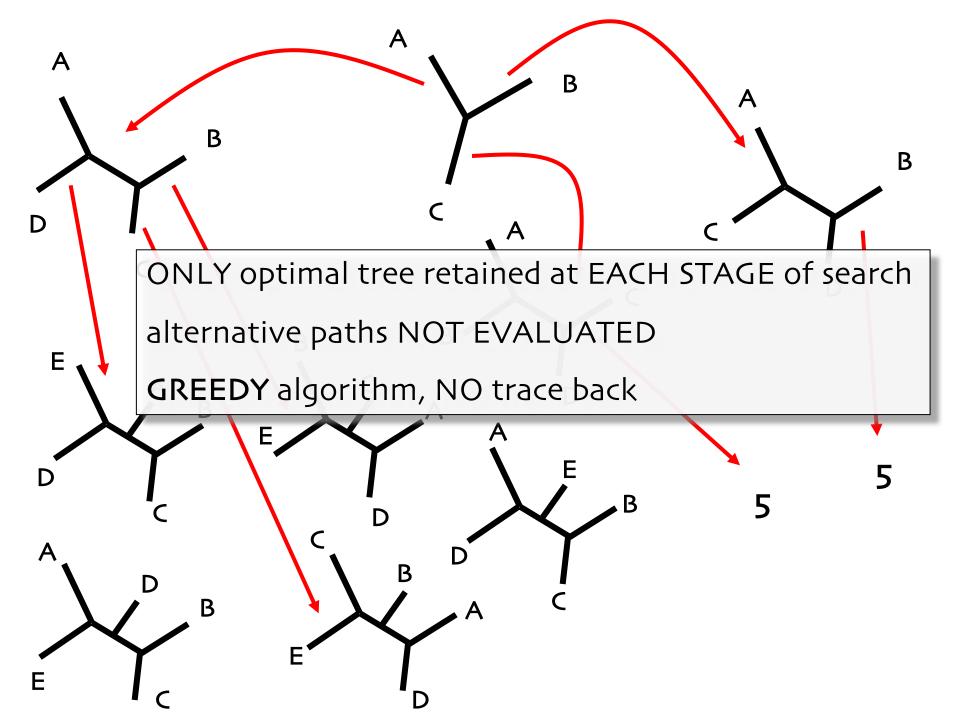
in practice ANY of the organisms can be used as outgroup

next search for a terminal to pair with it so that the number of observed **DIFFERENCES** between the two are minimized



the problem of Wagner algorithm is that the order where terminals are added to tree affects the tree finally obtained



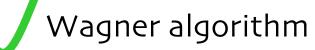


# HEURISTIC SEARCH

RAS = random addition sequence

1. starting trees built by adding terminals one by one

matrix/random order



phenetic clustering

all these can be combined to build starting trees

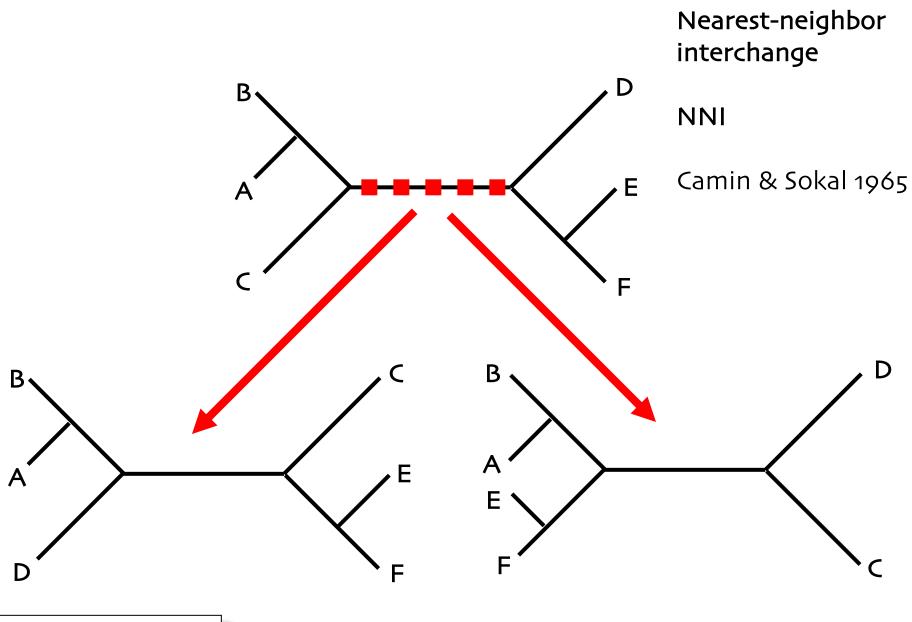
leads RARELY in finding shortest tree

# HEURISTIC SEARCH

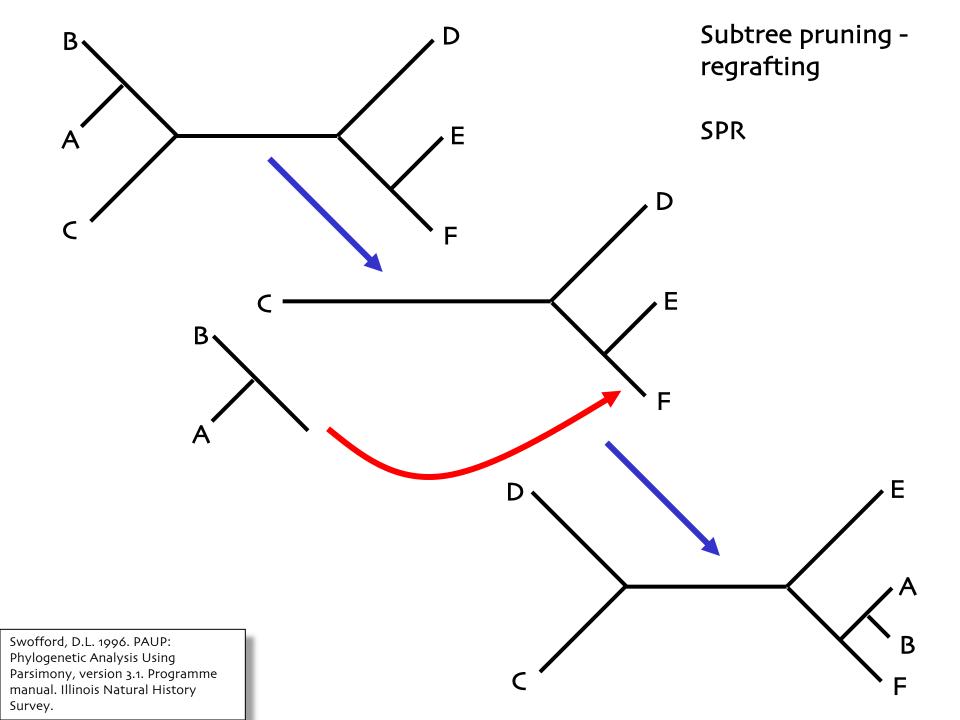
1. starting trees built by adding terminals one by one WAGNER algorithm

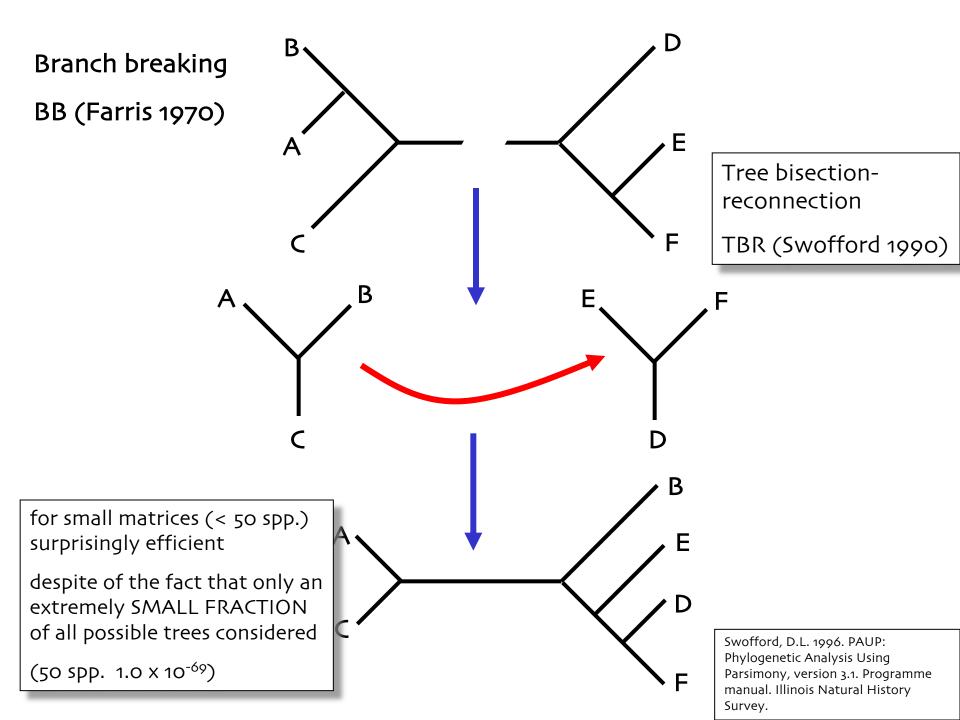
2. after this branches of the tree(s) are moved

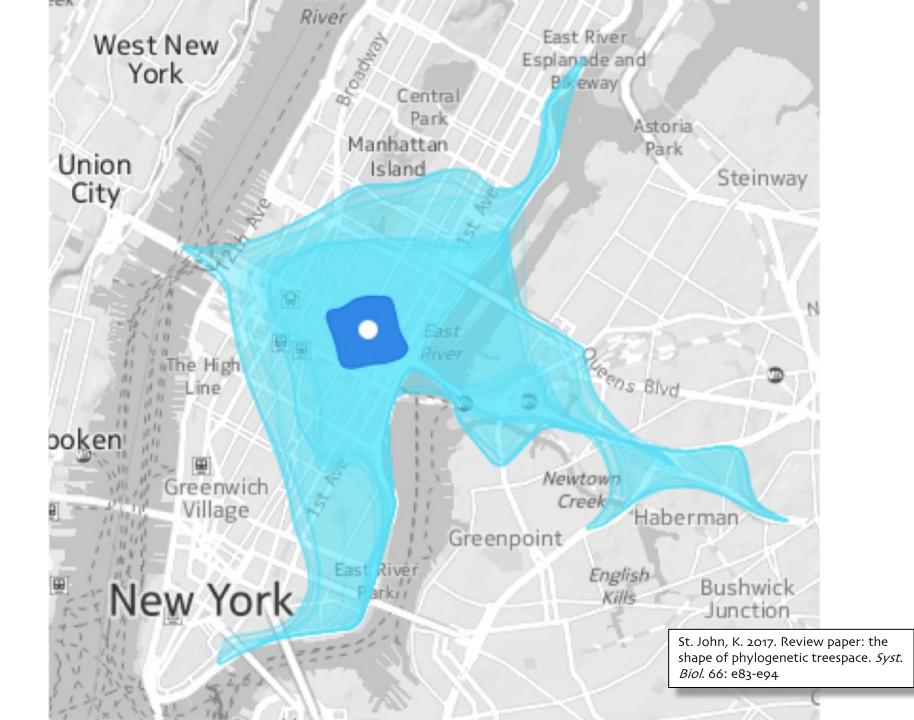
branch SWAPPING



Swofford, D.L. 1996. PAUP: Phylogenetic Analysis Using Parsimony, version 3.1. Programme manual. Illinois Natural History Survey.







# HEURISTIC SEARCH algorithms

ΝΝΙ	0 (n)	n = no. of lvs/terminals
SPR	O (n²)	
TBR	O (n³)	

## ....and in practice if we use RAS+TBR O ( $n^4$ )

Whidden, C. & Matsen IV, F.A. 2018. Efficiently inferring pairwise subtree prune-and-regraft adjacencies between phylogenetic trees. Proceedings of the meeting on analytical algorithmics and combinatorics: 77-91.

Wheeler 2017 (lecture notes CP217)

# HEURISTIC SEARCH

1. starting trees build by adding terminals one by one Wagner algorithm

2. after this branches of the tree(s) are moved

branch SWAPPING with NNI, SPR, TBR

3. current programs include algorithms that allow evaluation of tree length WITHOUT visiting ALL nodes of trees save processing time

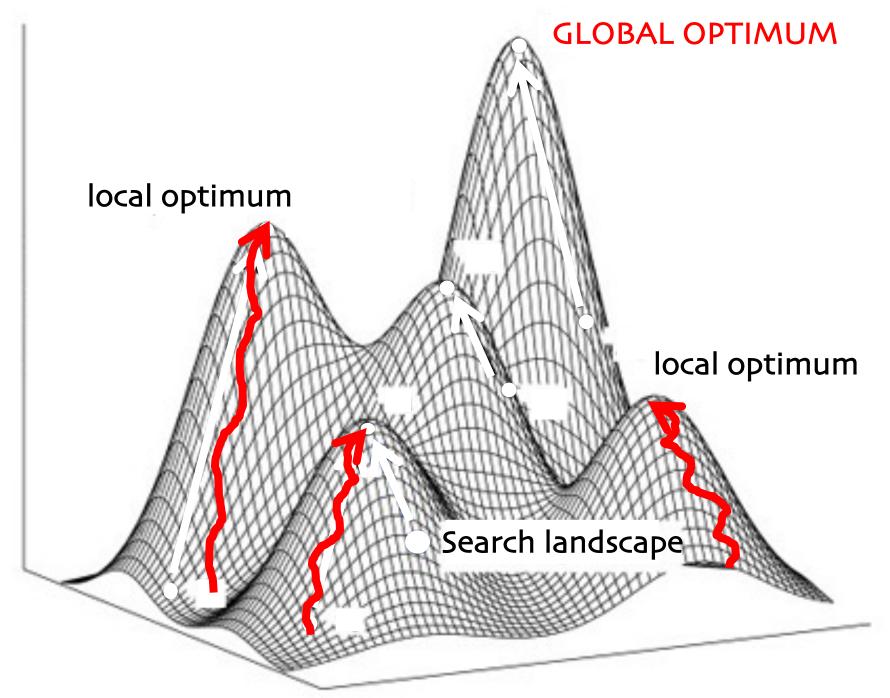
Goloboff, P.A. 1993. Character optimization and calculation of tree lengths. *Cladistics* 9: 433-436.

# Search strategies

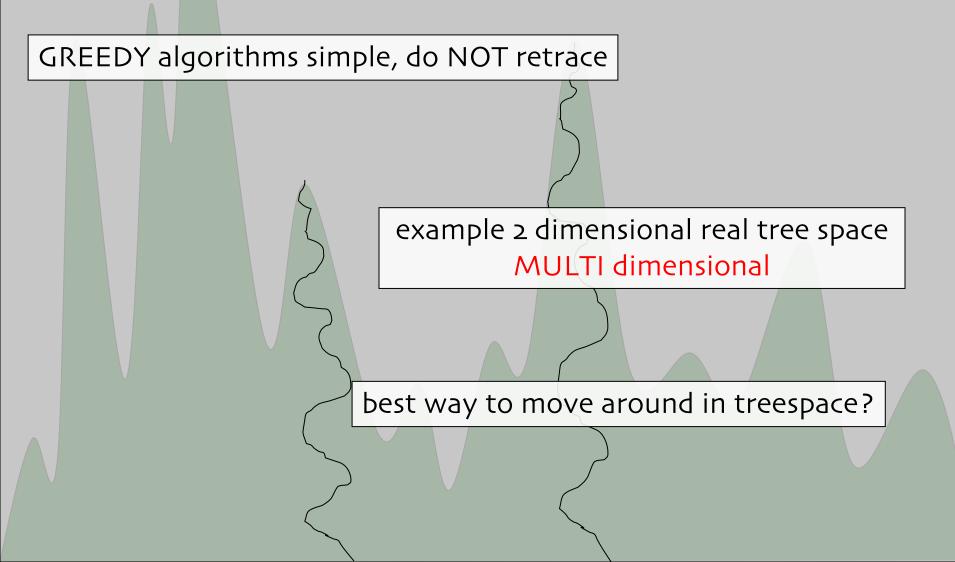
Maddison, D.R. 1991. The discovery and importance of multiple islands of most-parsimonious trees. *Syst. Biol.* 40: 315-328.

## islands of trees in tree "space" (landscape)

problem especially in analyses of larger matrices (> 100-200 terminals)



## greedy algorithms



# TRADITIONAL SEARCH STRATEGIES

search repeated SEVERAL TIMES (10 - 10 000 x)

how many times is sufficient?

has optimal tree be found?

if first 100x give same result **STOP** 

if only 1/100 give optimal result CONTINUE

moving branches takes time, thus the number of trees saved at intermediate stages of search kept

SMALL, e.g. <u><</u> 2-10 <sub>WHY?</sub>

when starting search potentially VERY DIFFERENT trees, after moving branches this is NOT anymore true, no reason to keep MANY SIMILAR trees most likely will lead finding same optimal tree

# TRADITIONAL SEARCH STRATEGIES

if > 10% of random searches give same result ---> search should be extended by expanding the number of trees saved in cache memory (50-100)

if < 10% random searches give same results ---> continue with NUMEROUS (500-1 000) additional random search repetitions with saving few trees in cache

finally 5-10% of trees saved in cache (50-200) analyzed in more detail

Davis, J. & al. 2005. The limits of conventional cladistic analysis. In: Albert, V. (ed.) *Parsimony, phylogeny and genomics*. 229 s. Oxford University Press

# TRADITIONAL SEARCH STRATEGIES

NO NEED to find ALL optimal trees (Farris & al. 1996)

for large matrices > 10° equally parsimonious trees might exist

consensus tree based only on small sample of trees might be identical with the one based on ALL trees if those sampled originate from SEPARATE tree groups

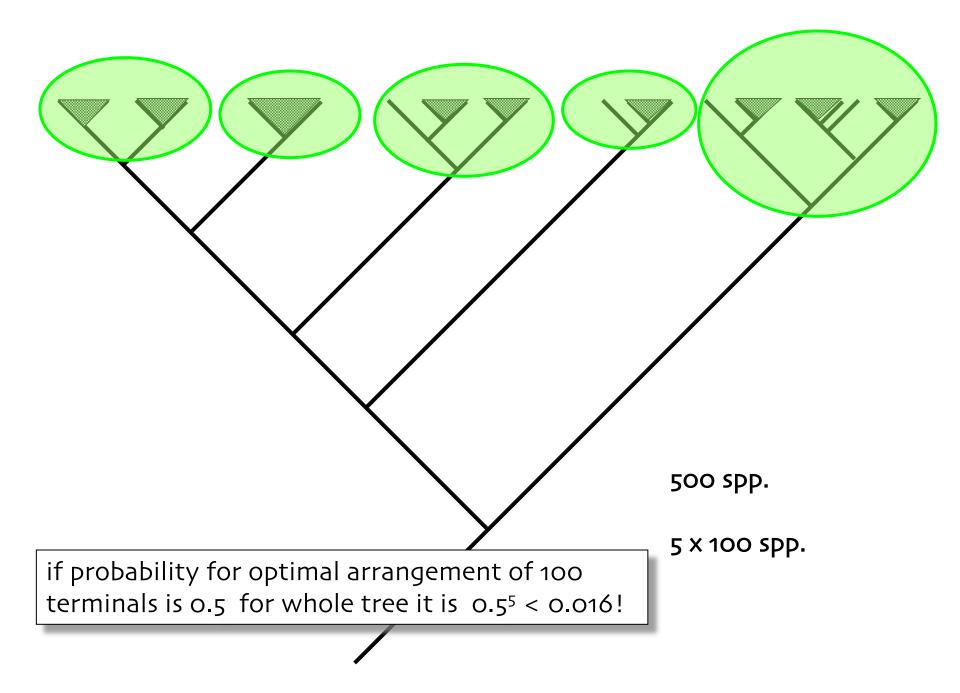
(islands)

can also be used to "guide" our search, i.e. if consensus does not change, no need to continue

# NEW SEARCH STRATEGIES

required for analyses of LARGE (> 500-700 spp.) matrices

in large trees ALL parts should be in optimal arrangement in order to be optimal as a WHOLE



#### GOLOBOFF 2000: dice comparison



www.weld-re1.k12.co.us/webclass/students/reamj/web/dice.gif

# NEW SEARCH STRATEGIES

Moilanen, A. 1999. Searching for most parsimonious trees with simulated evolutionary optimization. *Cladistics* 15: 39-50.

Nixon, K.C. 1999. The parsimony ratchet, a new method for rapid parsimony analysis. *Cladistics* 15: 407-414.

Goloboff. P.A. 1999. Analyzing large data sets in reasonable times: solutions for composite optima. *Cladistics* 15: 415-428.

# Nixon, K. Parsimony ratchet

diversityoflife.org/winclada/

1a. starting tree (e.g. Wagner algorithm)1b. continued using fast & simple branch swapping

weight = cost of ch. state change

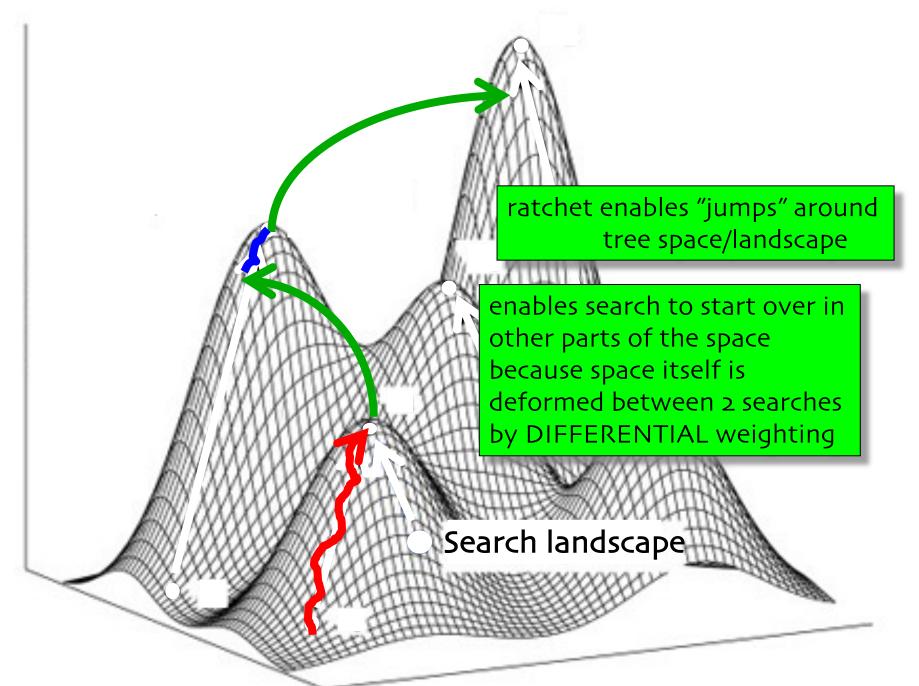
weight randomly e.g. 10-30% of characters
 try to find shortest tree of this NEW matrix (as in 1b)

4. return ORIGINAL weights

5. search for the shortest tree (as in 1b)6. return to 2. and repeat

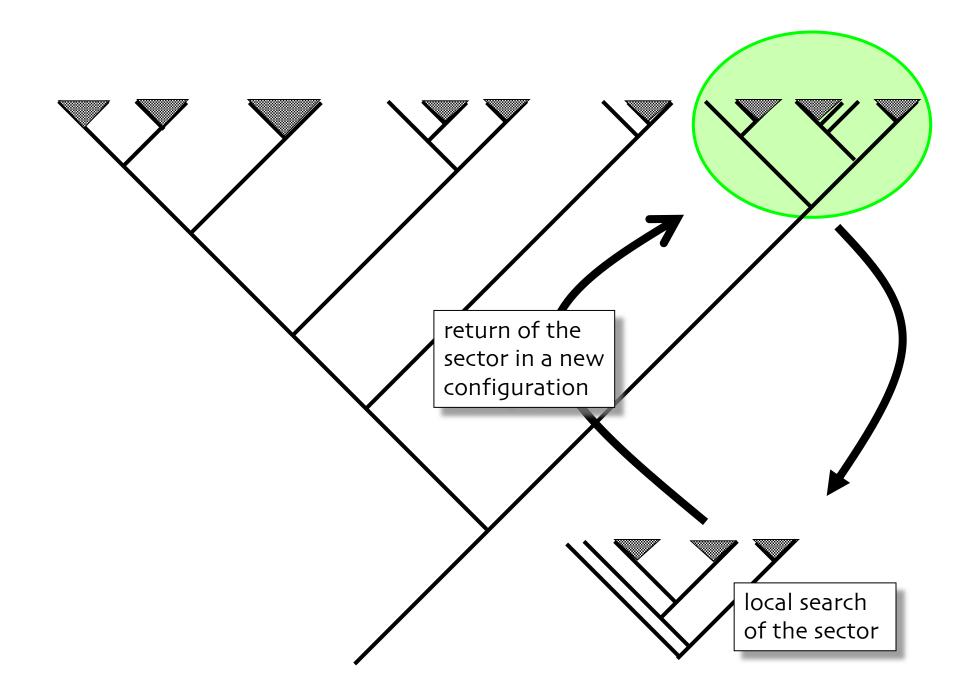
> 30x faster than traditional search strategies

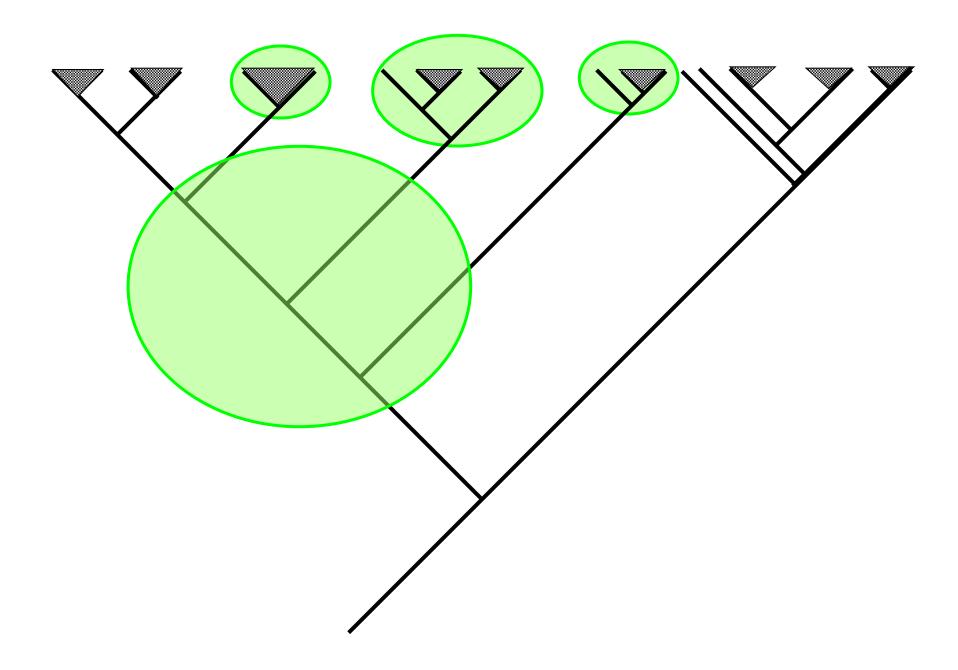
http://genealogyreligion.net/wp-content/uploads/2010/04/intelligencelandscape.jpg



# Goloboff, P. Sectorial search

- 1. part (a sector) of the tree found by traditional search chosen
- 2. a LOCAL search performed in this part & returned to original tree





# Goloboff, P. Sectorial search

- part (a sector) of the tree found by traditional search chosen
- 2. a LOCAL search performed in this part & returned to original tree
- 3. search performed numerous times with different parts
- 4. leads only rarely in finding optimal solution but MUCH faster than TBR

alternatives: RSS (random sectorial searches)

CSS (consensus-based sectorial s.)

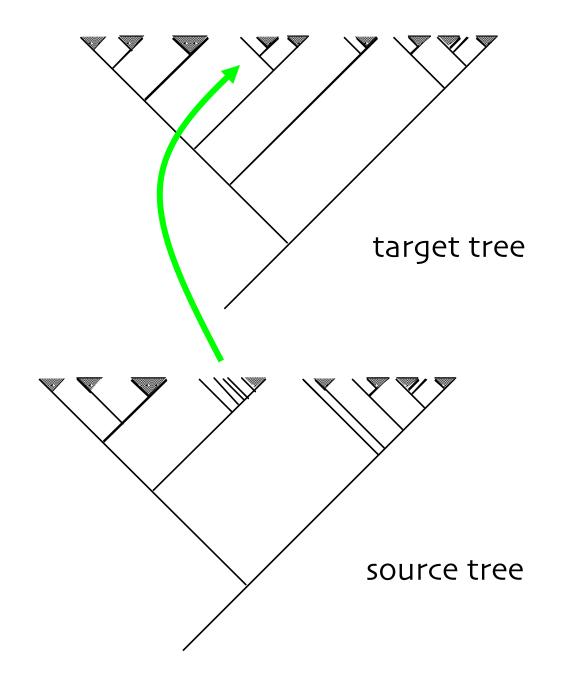
MSS (mixed sectorial s.)

CPU time increases LINEARLY in relation to number of sectors

EXPONENTIALLY in relation to number of terminals in TBR

# Goloboff, P. & Moilanen, A. Tree fusing

- 1. 2 starting trees chosen
- 2. trees compared sector by sector
- 3. all sectors of source tree that make target tree shorter are transferred to this latter tree



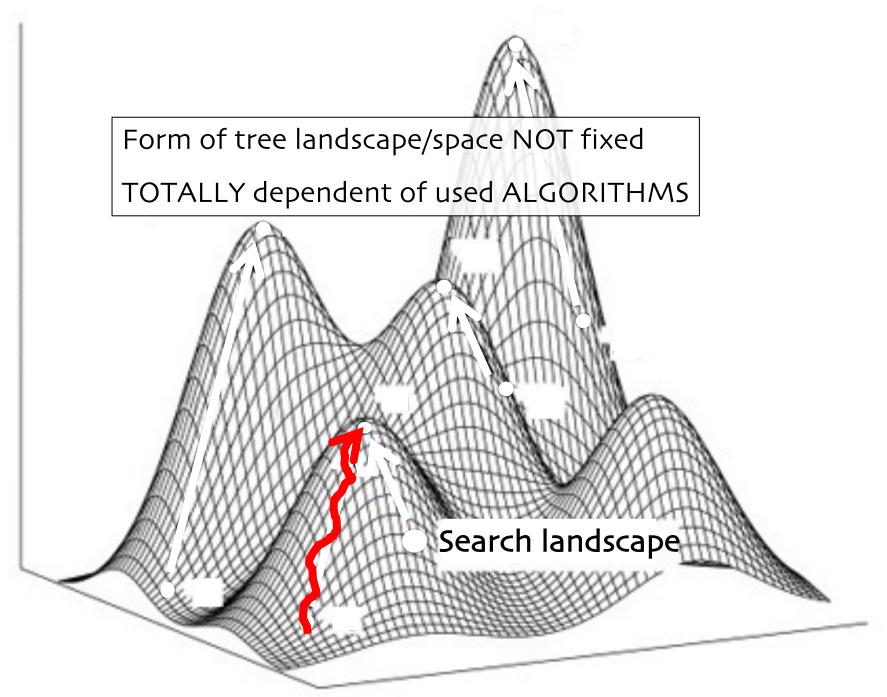
# Goloboff, P. (& Moilanen, A.) Tree fusing

- 1. 2 starting trees chosen
- 2. trees compared one sector at a time
- 3. all sectors that reduce tree length transferred from source to target tree
- 4. a new source tree chosen
- initially trees resulting from numerous searches needed
- efficiency of the method based on the fact that at least one part of the tree is in OPTIMAL configuration

# Goloboff, P. Tree drifting

*longer* than optimal trees accepted with predefined probability

widely known as "simulated annealing" used for analyses of difficult optimization problems





Cladistics

Cladistics 25 (2009) 1-20

10.1111/j.1096-0031.2009.00255.x

# Phylogenetic analysis of 73 060 taxa corroborates major eukaryotic groups

Pablo A. Goloboff<sup>a,\*</sup>, Santiago A. Catalano<sup>b</sup>, J. Marcos Mirande<sup>b</sup>, Claudia A. Szumik<sup>a</sup>, J. Salvador Arias<sup>a</sup>, Mari Källersjö<sup>c</sup> and James S. Farris<sup>d</sup>

<sup>a</sup>INSUE (Instituto Superior de Entomología), CONICET (Consejo Nacional de Investigaciones Científicas y Técnicas), Instituto Miguel Lillo, Miguel Lillo 205, 4000 S.M.Tucumán, Argentina; <sup>b</sup>CONICET (Consejo Nacional de Investigaciones Científicas y Técnicas), Fundación Miguel Lillo, Miguel Lillo 251, 4000 S.M.Tucumán, Argentina; <sup>c</sup>Göteborgs Botaniska Trädgård (Gothenburgh Botanical Garden), Carl Skottbergs Gata 22A, SE-413 19 Göteborg, Sweden; <sup>d</sup>Molekylärsystematiska laboratoriet, Naturhistoriska riksmuseet, Box 50007, 104-05 Stockholm, Sweden

Accepted 21 February 2009

#### Abstract

Obtaining a well supported schema of phylogenetic relationships among the major groups of living organisms requires considering as much taxonomic diversity as possible, but the computational cost of calculating large phylogenies has so far been a major obstacle. We show here that the parsimony algorithms implemented in TNT can successfully process the largest phylogenetic data set ever analysed, consisting of molecular sequences and morphology for 73 060 eukaryotic taxa. The trees resulting from molecules alone display a high degree of congruence with the major taxonomic groups, with a small proportion of misplaced species; the combined data set retrieves these groups with even higher congruence. This shows that tree-calculation algorithms effectively

# Concluding remarks

solutions to find optimal trees varies according to the data analyzed

e.g. extensive homoplasy vs. randomly sparse matrices

increasingly common with large genetic materials

Wagner algorithm used initially to find starting trees

modified | selected/informative addition

Goloboff, P.A. 2014. Hide and vanish: data sets where the most parsimonious tree is known but hard to find, and their implications for tree search methods. *Mol. Phyl.& Evol.* 79: 118-131.

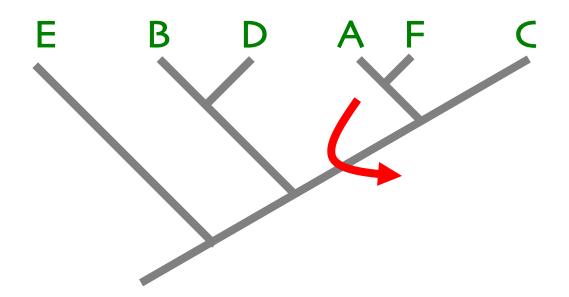
# 7.xi.

- 1. search algorithms
- 2. traditional search strategies
- 3. new search strategies

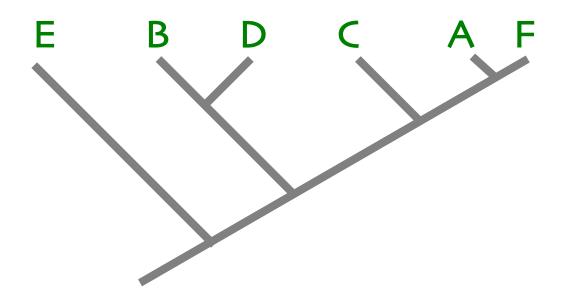
#### 4. tree form and consensus & compromise trees

5. summary

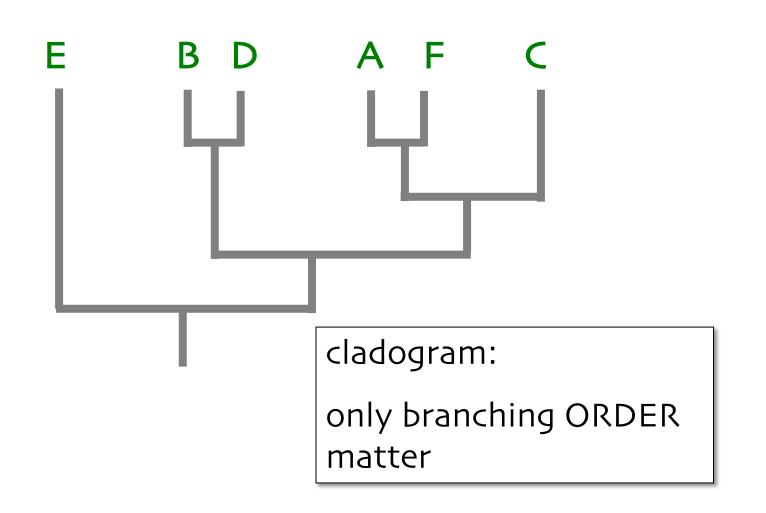
### TREES & their form

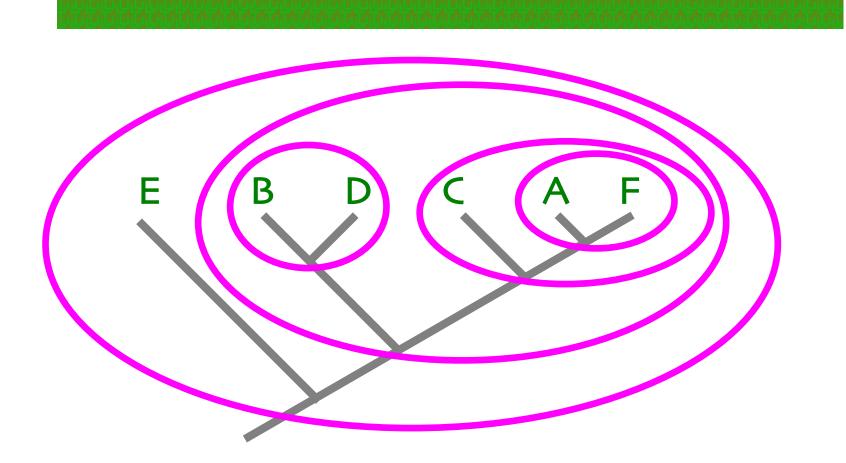


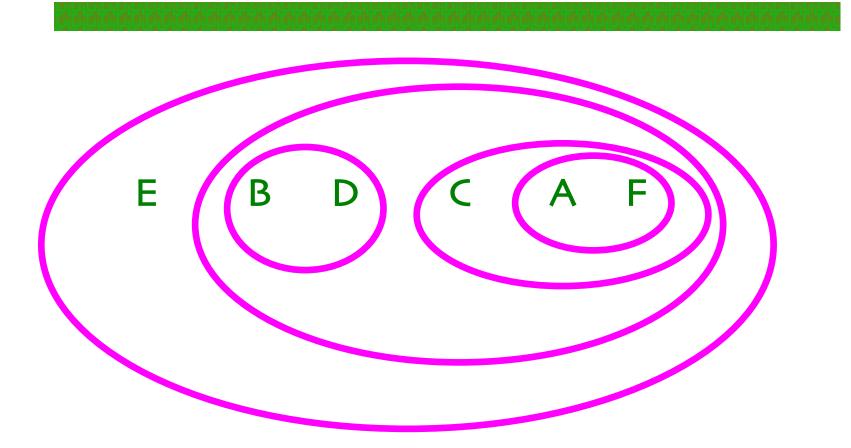
### TREES & their form

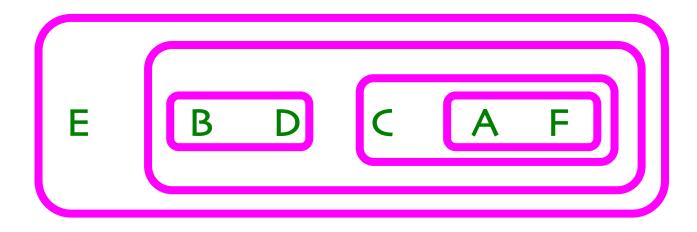


# TREES & their form









Venn diagram

# E (B D) (C (A F))

From Venn diagram ---->

# (E ((B D) (C (A F))))

parenthetical notation

Enables presentation of trees as part of normal text

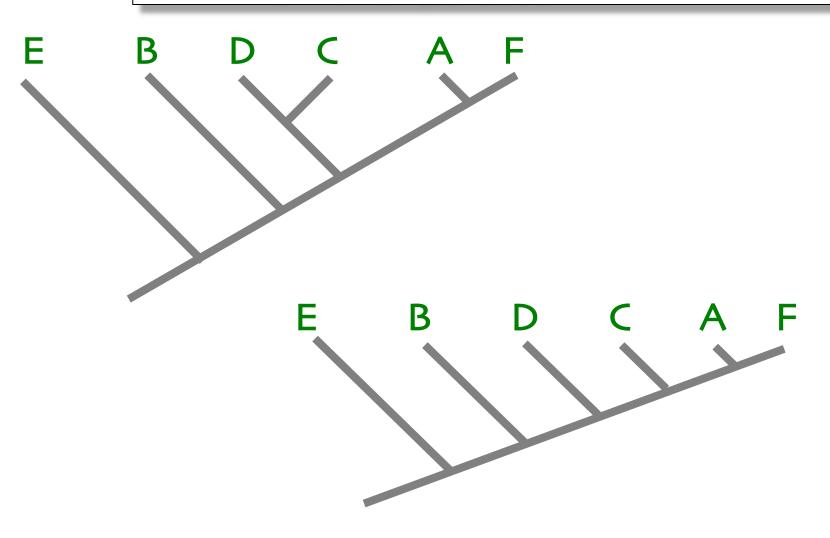
#### (E ((B D) (C (A F))))

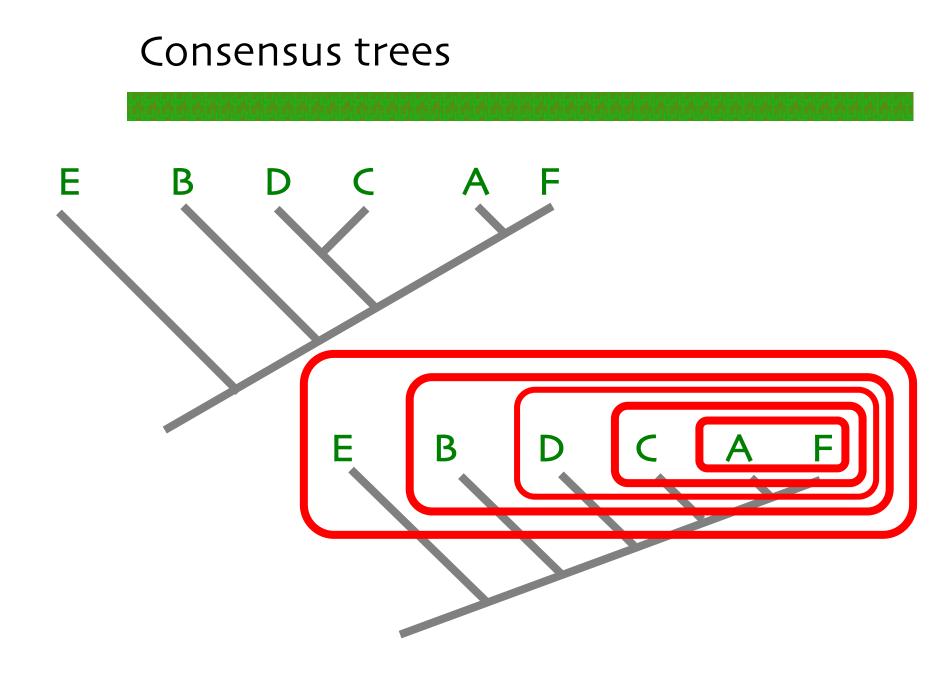
naturally used also in programming

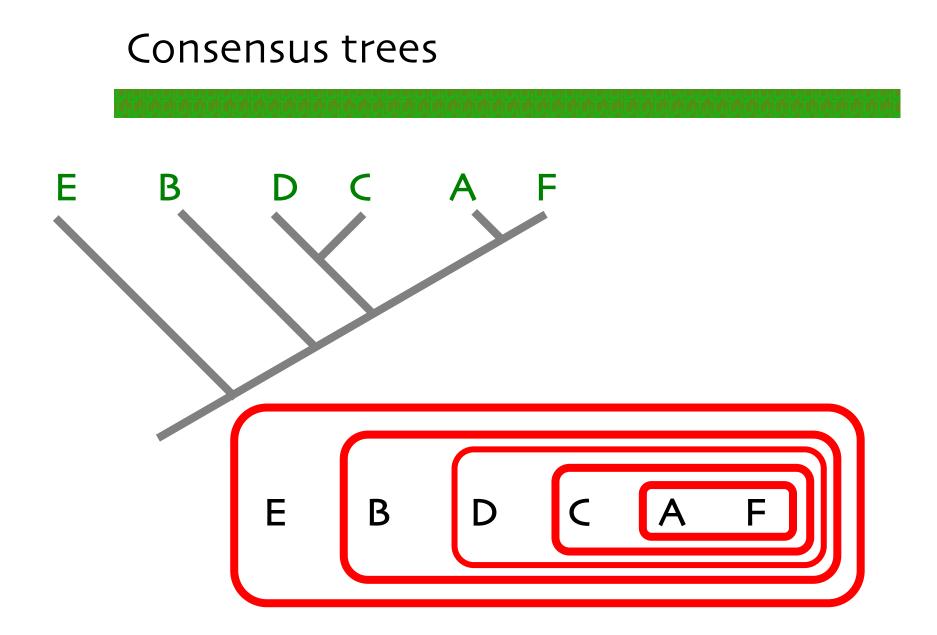
# Consensus & compromise trees

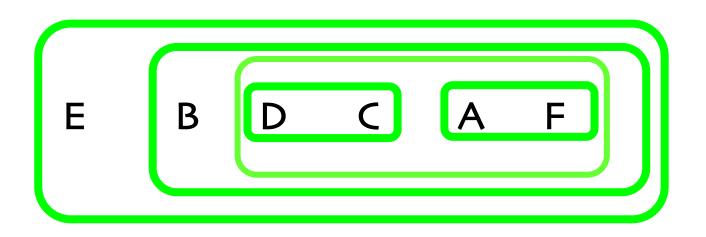
ONLY trees treated & compared, **NOT CHARACTERS** 

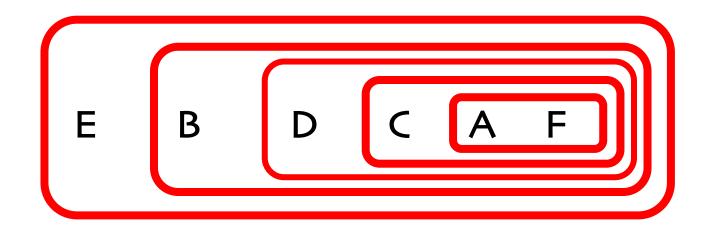
Sokal, R. R. & Rohlf, F. J. 1981. Taxonomic congruence in the Leptopodomorpha re-examined. *Systematic Zoology* 30: 309-325.

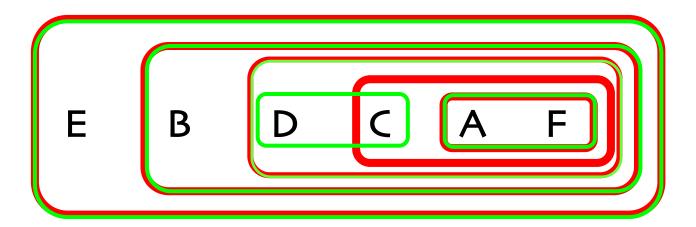


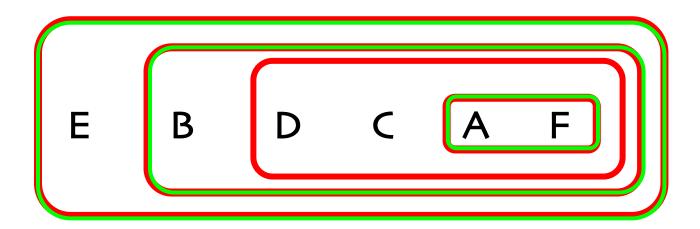


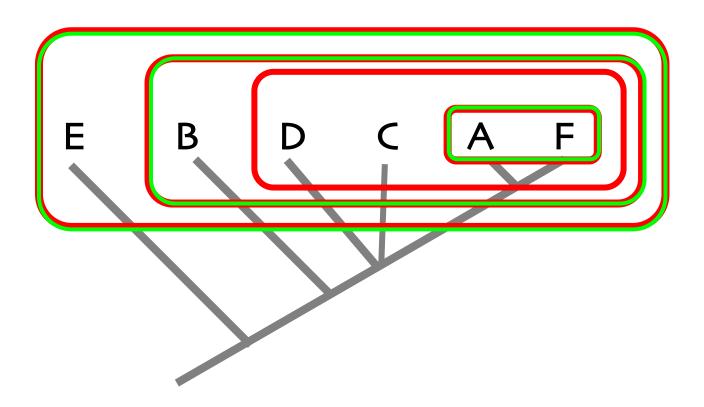


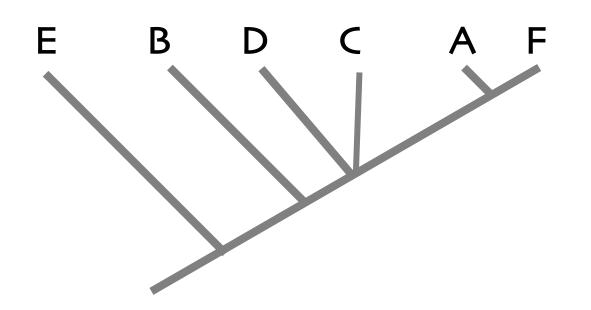


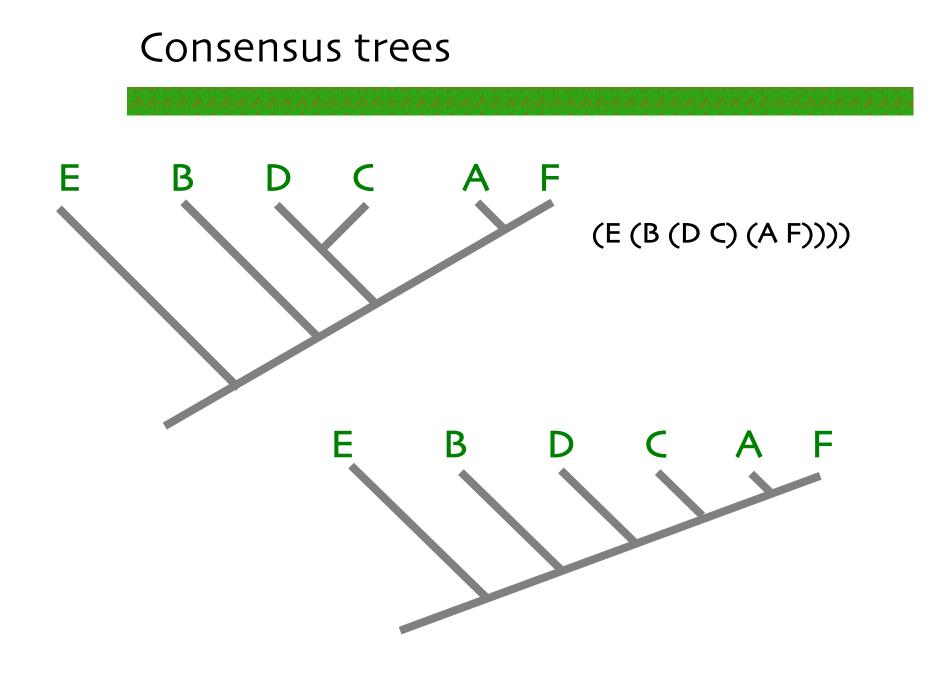


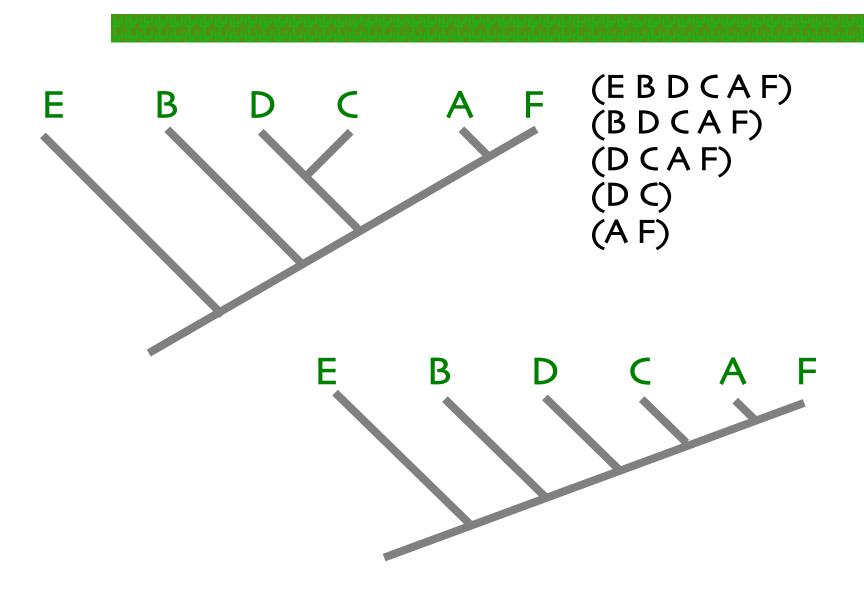


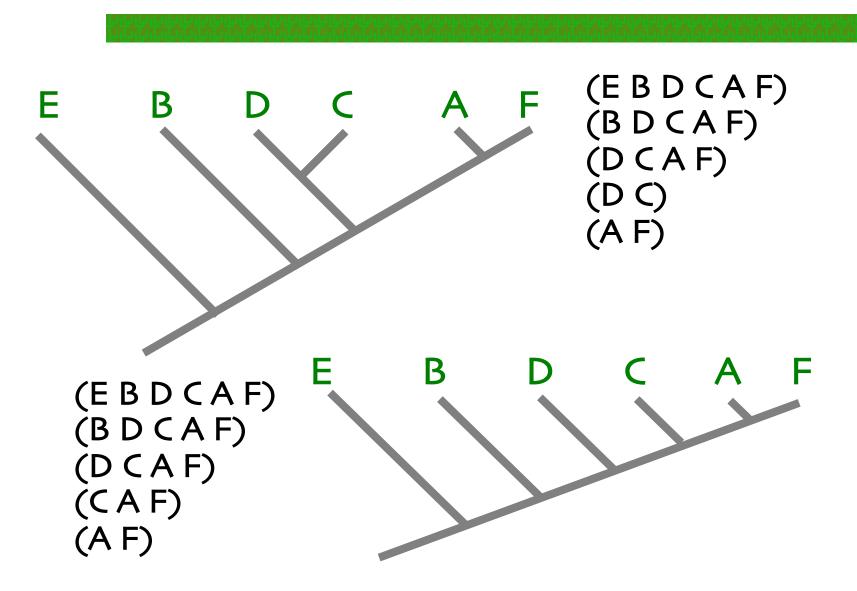


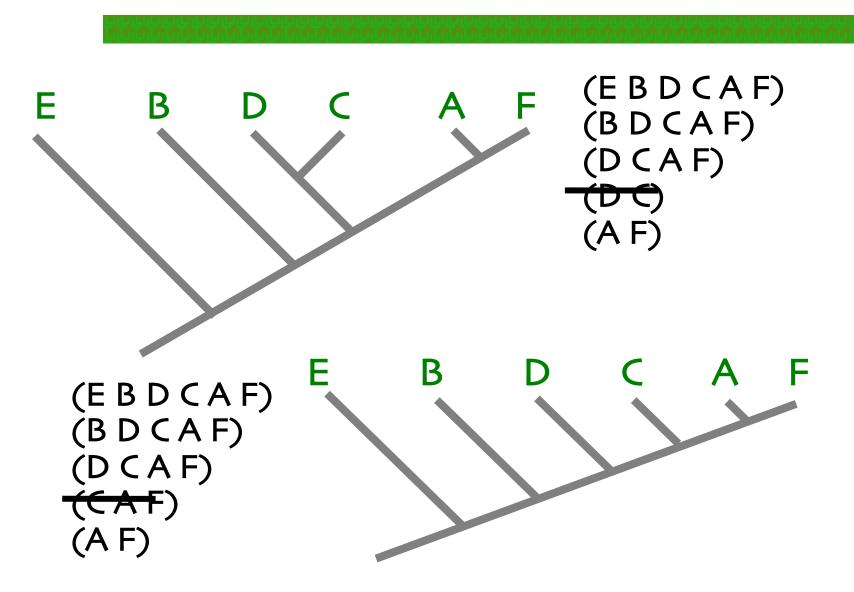






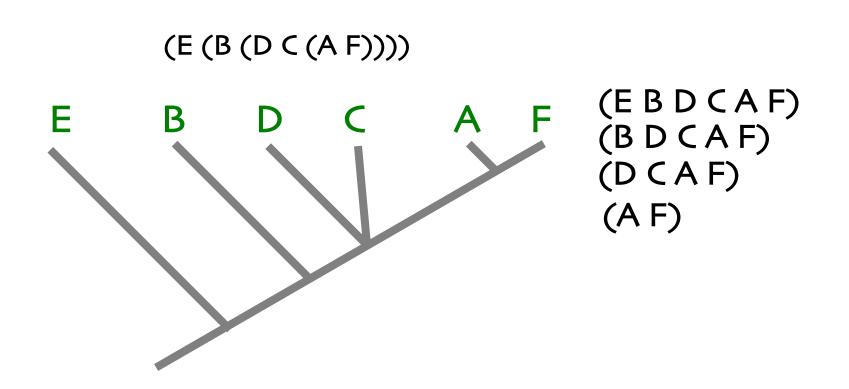






### (E (B (D C (A F))))

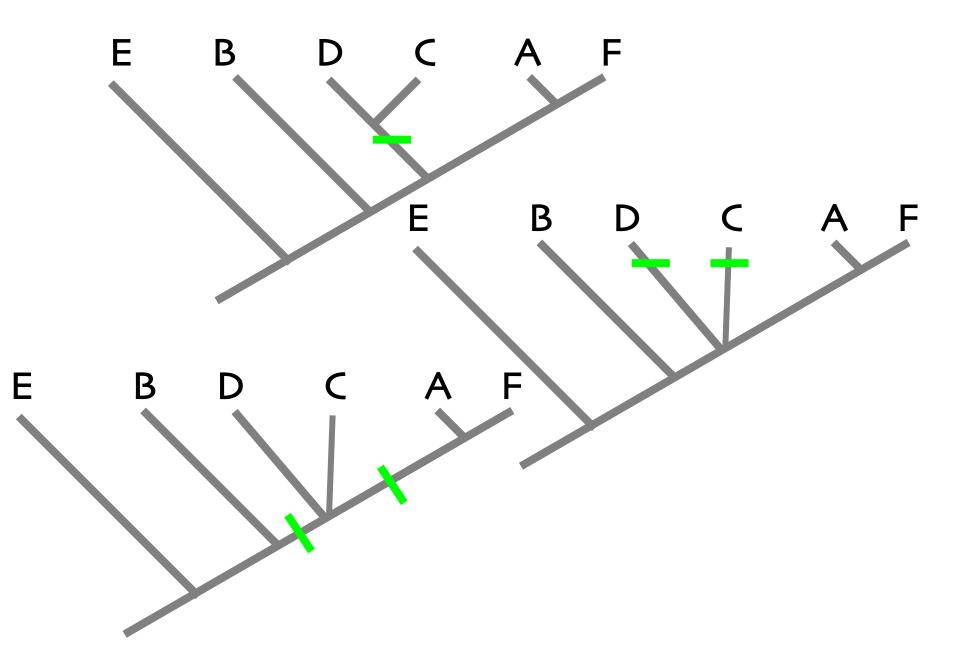
## (E B D C A F) (B D C A F) (D C A F) (A F)

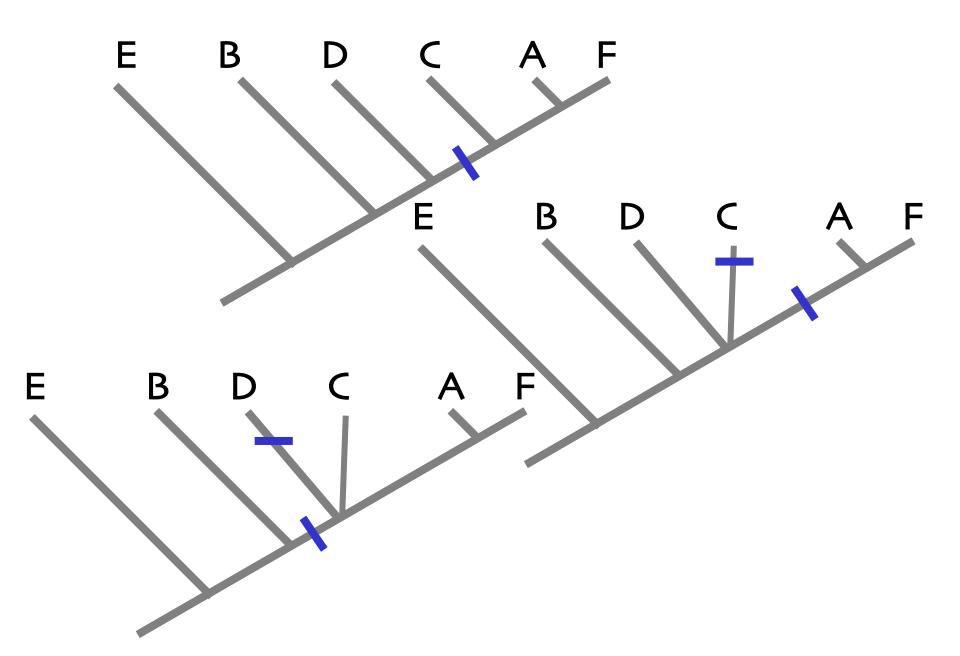




#### consensus tree is <u>ALWAYS ONLY SUMMARY</u>

# it is <u>ALWAYS more complicated</u> than any of the original trees







consensus tree is <u>ALWAYS ONLY SUMMARY</u>

it is <u>ALWAYS more complicated</u> than any of the original trees groups shared by ALL trees are presented on 1 tree



Majority rule compromise

Adams

Combinable component (semistrict)

Nixon, K. C. & Carpenter, J. 1996. On consensus, collabsibility, and clade concordance. *Cladistics* 12: 305-321.

## COMPROMISE TREES

#### Majority rule compromise

Margush, T. & McMorris, F. R. 1981. Consensus n-trees. Bull. Math. Biol. 43: 239-244.

Adams

Combinable component (semistrict)

## COMPROMISE TREES

commonly used for presentation of support values

mostly those groups present on  $\geq$  50% of original trees included

percentage describing the presence of groups marked on compromise tree (50-100)

## COMPROMISE TREES

majority rule compromise

when used as summary of optimal trees it should be noticed that part of the original trees are in **CONFLICT** with this summary!!

this kind of usage <u>IS NOT RECOMMENDED</u>, simply MISLEADING

## SUMMARY

exhaustive & branch and bound searches can be used only for analyses of SMALL matrices only these two ENSURE finding the optimal tree

heuristic search is based on rearrangement of branches

of tree(s) branch SWAPPING

searches should be planned carefully BEFORE starting them in order to avoid unnecessary analyses of large number of similar trees & use of CPU time

use of best programs & efficient algorithms necessary for analyses of LARGE matrices

PARALLELIZATION have enabled analyses of larger and larger materials

trees can be presented as PARENTHETICAL NOTATIONS consensus trees are useful **SUMMARIES** of many trees