

Self-Catalytic Reaction of SO₃ and NH₃ To Produce Sulfamic Acid and Its Implication to Atmospheric Particle Formation

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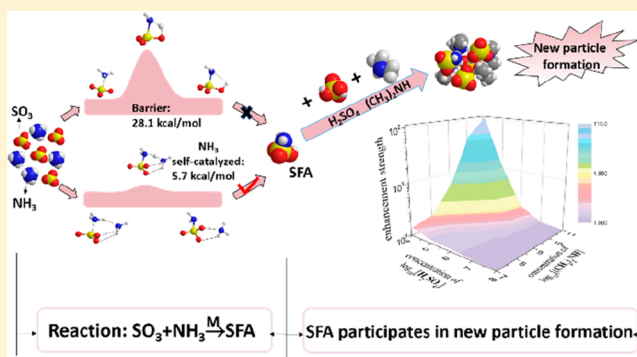
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Supporting Information

ABSTRACT: Sulfur trioxide (SO₃) is one of the most active chemical species in the atmosphere, and its atmospheric fate has profound implications to air quality and human health. The dominant gas-phase loss pathway for SO₃ is generally believed to be the reaction with water molecules, resulting in sulfuric acid. The latter is viewed as a critical component in the new particle formation (NPF). Herein, a new and competitive loss pathway for SO₃ in the presence of abundant gas-phase ammonia (NH₃) species is identified. Specifically, the reaction between SO₃ and NH₃, which produces sulfamic acid, can be self-catalyzed by the reactant (NH₃). In dry and heavily polluted areas with relatively high concentrations of NH₃, the effective rate constant for the bimolecular SO₃–NH₃ reaction can be sufficiently fast through this new loss pathway for SO₃ to become competitive with the conventional loss pathway for SO₃ with water. Furthermore, this study shows that the final product of the reaction, namely, sulfamic acid, can enhance the fastest possible rate of NPF from sulfuric acid and dimethylamine (DMA) by about a factor of 2. An alternative source of stabilizer for acid–base clustering in the atmosphere is suggested, and this new mechanism for NPF has potential to improve atmospheric modeling in highly polluted regions.



INTRODUCTION

Sulfur trioxide (SO₃) is a major air pollutant^{1–5} and is mainly produced by the gas-phase oxidation of SO₂.^{6,7} As a highly reactive gas⁸ and one of the most common acid oxides, SO₃ can lead to both acid rain and atmospheric aerosol^{9–13} and thus has important implications for regional climate and human health.^{14–19} The reaction between SO₃ and water (H₂O) has been generally considered as the dominant pathway for the loss of SO₃ because the H₂O concentration is ~10¹⁷ molecules cm⁻³ in the boundary layer, which is several orders of magnitude greater than that of other condensable gases.²⁰ The relevant reaction equation can be described by **reaction 1**:



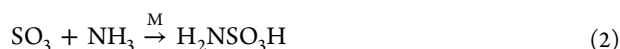
Both experimental and theoretical studies^{21–26} indicate that a facilitator molecule M, acting as a catalyst, is required. For example, previous experiment study by Jayne et al.²³ showed that **reaction 1** exhibits second-order dependence on water vapor concentration, and other previous theoretical studies²² indicated the addition of a second water molecule could substantially lower the activation barrier. More recently, sulfuric acid (SA)²⁴ or other atmospheric molecules (such as formic acid²⁵ or ammonia²⁶) make the reactions barrierless and thus significantly fast. However, in highly polluted regions, the concentration of NH₃ can reach 105.0 μg m⁻³ (or ~3.7 × 10¹² molecules cm⁻³).²⁷ Furthermore, in relatively dry conditions or at lower temperatures, e.g., in the winter, the

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concentration of gas-phase water molecules is drastically reduced.¹³ Hence, SO₃ may react with NH₃ before reacting with H₂O.

The possibility of an SO₃–NH₃ reaction was previously studied in the laboratory, and its effective rate coefficient was detected to be 10^{–12}–10^{–10} cm³ molecule^{–1} s^{–1} at NH₃ concentration of 10¹¹–10¹³ molecules cm^{–3}.^{28–32} Such unexpectedly high values of the rate coefficient are similar to those of SO₃ and water dimer reaction (10^{–11}–10^{–10} cm³ molecule^{–1} s^{–1}),^{21–23,33} implying that the reaction with NH₃ might be an important sink of SO₃. A Fourier-transform infrared spectroscopy (FTIR) study by Hirota et al.³⁰ showed that with NH₃ the product from the reaction of SO₃ was sulfamic acid (H₂NSO₃H, SFA). Previous theoretical studies^{34,35} predicted that a direct SO₃–NH₃ reaction was kinetically unfavorable because of the high reaction barrier (28.6 kcal/mol). The discrepancy between theoretical and experimental results suggests that this reaction might require a facilitator molecule M, as in reaction 2:



Thus, it is important to determine whether reaction 2 entails a much lower reaction barrier with either another NH₃ molecule or the SFA molecule as a catalyst, and also important to elucidate the underlying reaction mechanism.

From the perspective of its structure, SFA possesses two functional groups: a sulfonic acid and an amino group. Both groups can act as hydrogen donors and acceptors to interact with atmospheric particle precursors as proven by previous works.^{36–39} Furthermore, in the experiment performed by Lovejoy et al.,²⁹ SFA was observed to cluster efficiently with itself and SA, indicating its potential for aerosol new particle formation (NPF). Although several compounds have been identified in promoting NPF process, they are mostly correlated with special environment, for example, highly oxidized multifunctional organic molecules (HOMs) mostly in forest, rural, and urban areas,^{40–43} iodic acid (HIO₃) in coastal area and open ocean region,⁴⁴ and methanesulfonic acid (MSA) mostly in marine region.⁴⁵ A main question that we intend to address here is whether SFA produced by the reaction between SO₃ and NH₃ is capable of enhancing the nucleation of SA and base (i.e., ammonia or amine) molecular clusters, in view of that the latter species have been recognized as dominant precursors in highly polluted areas, especially in some megacities in Asia.^{46–53}

In this work, using high-level theoretical methods, we first studied the reaction between SO₃ and NH₃ to form SFA with the reactant (NH₃) or product (SFA) being considered as a self- or autocatalyst. Next, we used the Atmospheric Clusters Dynamic Code (ACDC)⁵⁴ to investigate how the product (SFA) is involved in SA-dimethylamine (SA-DMA)-based cluster formation. Particular attention of this work is placed on the study of (1) the possibility of the SO₃ and NH₃ reaction functioning as an important loss pathway in highly polluted areas with high NH₃ concentrations and (2) the fate of the product in atmospheric NPF and the influence of various environmental conditions.

METHODS

Quantum Chemical Calculation. All density functional theory (DFT) calculations were performed with using Gaussian 09⁵⁵ software packages. For all reactions involving SO₃ and NH₃, structure optimization and subsequent frequency analysis of the stationary

points were carried out at the M06-2X/6-311++G(3df,3pd) level of theory. Several previous studies^{36–39,56} have shown that the M06-2X functional is an accurate DFT method for computing thermochemistry, kinetics, and noncovalent interactions involving the main-group elements. Intrinsic reaction coordinate (IRC) was also calculated to ensure the correct transition states for the products and reactants. Single-point energies for the stationary points were computed using the ORCA 3.03 Package⁵⁷ to obtain more reliable energies. To this end, the explicitly correlated coupled cluster (CCSD(T)-F12)⁵⁸ method with the cc-pVDZ-F12 basis set⁵⁹ and appropriate auxiliary basis sets were used.

For the chemical processes involving interactions between SFA and other precursors resulting in particle formation, a systematic sampling technique was used to search for the global minima of the molecular clusters. In the first step, a thousand structures are autogenerated using the ABCluster⁶⁰ software with the TIP4P^{61,62} model for water molecules and the CHARMM⁶³ force field for others; these structures were then preoptimized based on the semiempirical method (PM7) with Mopac2016.^{64,65} Next, up to 100 low-energy conformations were reoptimized using the M06-2X/6-31+G* level of theory to determine the ten lowest-lying structures, followed by another optimization with using the larger 6-311++G(3df,3pd) basis set to determine the global minimum. The Cartesian coordinates and the corresponding formation Gibbs free energy of the stable clusters are summarized in the Supporting Information.

Atmospheric Clusters Dynamic Code (ACDC) Model. The ACDC⁵⁴ kinetic model with the MATLAB-R2013a⁶⁶ program is used to compute the time evolution of formation rates and growth paths of the clusters. For a given set of atmospheric clusters, the code can be used to solve the birth–death equations (see eq 3 below) with calculated formation free energies (based on other theoretical method) as the inputs. The overall process accounts for all possible collision and evaporation of the relevant clusters. Specifically, the birth–death equation is written as

$$J = \frac{dc_i}{dt} = \frac{1}{2} \sum_{j < i} \beta_{j,(i-j)} c_j c_{(i-j)} + \sum_j \gamma_{(i+j) \rightarrow i} c_{i+j} - \sum_j \beta_{i,j} c_i c_j - \frac{1}{2} \sum_{j < i} \gamma_{i \rightarrow j} c_i + Q_i - S_i \quad (3)$$

where J refers to the cluster formation rate, i (or j) is a molecule or a cluster, c_i stands for the concentration of i , β_{ij} and $\gamma_{i+j \rightarrow i}$ are the collision coefficient of i with j or the evaporation coefficient of $i + j$ cluster evaporating into i and j , respectively. Q_i , set to be zero in the present study, is the possible other source of i . S_i represents the sink term of i .

The collision coefficient β_{ij} is based on the kinetic gas theory^{67,68} and eq 4:

$$\beta_{i,j} = \left(\frac{3}{4\pi} \right)^{1/6} \left(\frac{6k_b T}{m_i} + \frac{6k_b T}{m_j} \right)^{1/2} (V_i^{1/3} + V_j^{1/3})^2 \quad (4)$$

where m_i and V_i are the mass and volume of i , and similarly, m_j and V_j are the mass and volume of j , respectively, which are calculated via eq 5

$$V = \left(\frac{4}{3} \right) \pi (r)^3 \quad (5)$$

where r is the molecular radius derived by using Multiwfn software.⁶⁹ More details can be found from our previous paper.⁷⁰

The evaporation coefficient $\gamma_{(i+j) \rightarrow i}$ was calculated using the formation Gibbs free energies of the given clusters and eq 6

$$\gamma_{(i+j) \rightarrow i} = \beta_{i,j} \frac{c_i^e c_j^e}{c_{i+j}^e} = \beta_{i,j} c_{\text{ref}} \exp \left\{ \frac{\Delta G_{i+j} - \Delta G_i - \Delta G_j}{k_b T} \right\} \quad (6)$$

where c_i^e refers to the equilibrium concentration of i , ΔG_i is the formation free energy of i , and c_{ref} represents the monomer

concentration of the reference vapor at a pressure of 1 atm, which is the pressure at which the Gibbs free energies are determined.

Generally, the simulation system is regarded as an “ $a \times b$ ” box, where a or b is the maximum number of acid or base molecules of the clusters, respectively. Here, the cluster size of the simulated systems was set to be 3×2 , containing $(\text{SFA})_x(\text{SA})_y(\text{DMA})_z$ (where the sum of x and y from 0 to 3, z from 0 to 2) clusters. The mobility diameter of the largest cluster is 1.7 nm, which is chosen because the NPF rates typically use this standard during experimental measurement.⁷¹ Among these clusters, only the clusters including an equal numbers of base and acid molecules or the clusters with smaller numbers of base than acid molecules were considered, as only these clusters have the potential to further grow into larger sizes.⁷² In addition, considering the formation Gibbs free energy (Table S1) and evaporation rates (Table S2), the clusters containing SA and DMA molecules and an SFA molecule are the most stable and are therefore allowed to grow to larger clusters, thereby contributing to the rate of NPF. Given the above considerations, clusters $(\text{SA})_3(\text{DMA})_3$ and $\text{SFA} \cdot (\text{SA})_2 \cdot (\text{DMA})_3$ are set as the boundary clusters. Moreover, the coagulation sink coefficient is set to be $5 \times 10^{-2} \text{ s}^{-1}$ in the case of polluted areas.^{73–75}

RESULTS AND DISCUSSION

Reactant as Self-Catalyst and Product as Autocatalyst. A previous theoretical study³⁴ showed that the direct reaction between SO_3 and NH_3 without a catalyst is not a plausible path for SFA formation due to a high reaction barrier (Figure 1a). The high barrier is a consequence of large ring tension of the rather closed four-membered ring transition-state geometry, making SFA formation kinetically unfavorable. However, previous experimental studies^{28,29} indicated that the bimolecular rate coefficient for the $\text{SO}_3\text{--NH}_3$ reaction can reach $\sim 10^{-10} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$. Such a high reaction rate coefficient reflects a fast and easy reaction. The apparent inconsistency between experimental measurement and theoretical prediction suggests that the reaction between SO_3 and NH_3 may involve a catalyst. Thus, we first examine the SFA formation from the SO_3 and NH_3 reaction with either the NH_3 reactant or the SFA product as a catalyst. As shown in Figure 1b, with the reactant (NH_3) acting as a catalyst, the reaction barrier is substantially lower than that of the direct reaction (Figure 1a). Reactions starting with the formation of different dimers among two of three molecules (SO_3 , NH_3 , and NH_3 molecules) were examined, and the $\text{SO}_3\text{·NH}_3$ heterodimer was expected to be the best candidate due to its most negative Gibbs free energy of formation ($-10.0 \text{ kcal mol}^{-1}$) among the possible dimers. Next, the reaction continues to yield a prereactive complex C2 with a formation free energy of $-12.4 \text{ kcal mol}^{-1}$, followed by the formation of a hydrogen-bonded complex P2 via TS2 transition state, with a free energy barrier of $5.7 \text{ kcal mol}^{-1}$. The NH_3 molecule in TS2 acts as a double donor and a single acceptor of hydrogen to form a steric network with an $\text{SO}_3\text{·NH}_3$ heterodimer through van der Waals interactions. As a result, the ring strain of the transition state is reduced with increasing ring size from a four-membered ring structure to a cage-like hydrogen-bonding network; the associated energy barrier is significantly lower than that without the self-catalyst. Hence, the reactant self-catalysis mechanism for the $\text{SO}_3\text{--NH}_3$ reaction is predicted.

In addition to the reactant (NH_3) self-catalysis mechanism, the SFA autocatalysis mechanism (Figure 1c) can also facilitate the formation of SFA with high efficiency. The reaction barrier involved is $9.0 \text{ kcal mol}^{-1}$, which is also much lower than that without the autocatalyst (Figure 1a). This autocatalysis reaction can, in principle, begin with three primary paths

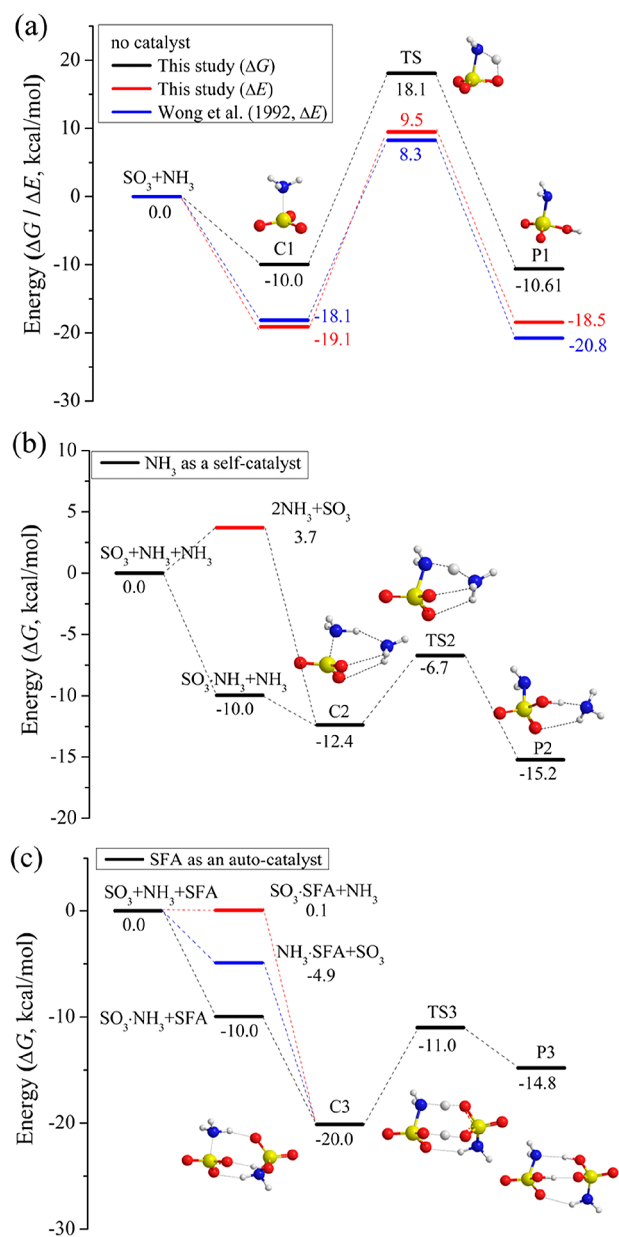


Figure 1. Potential energy surfaces for the reaction of SO_3 and NH_3 with (a) no catalyst; (b) NH_3 as a self-catalyst; and (c) SFA as an autocatalyst. Hydrogen, oxygen, sulfur, and nitrogen atoms are represented by gray, red, yellow, and blue spheres, respectively. C, TS, and P refer to prereaction complex, transition state, and product, respectively.

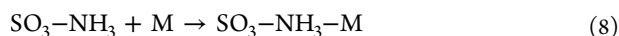
involving the bimolecular collision between an NH_3 molecule and an SO_3 molecule, a collision between an SO_3 molecule and an SFA molecule, or a collision between an SFA molecule and an NH_3 molecule. However, Figure 1c shows that the first path is most likely due to the greater stability of $\text{SO}_3\text{·NH}_3$ heterodimer among the three possible first formed dimers. Thus, the reaction starting with the formation of an $\text{SO}_3\text{·NH}_3$ heterodimer, followed by the formation of a prereactive complex C3, with a formation free energy of $-20.0 \text{ kcal mol}^{-1}$ (much lower than the value for C2 ($-12.4 \text{ kcal mol}^{-1}$)) indicates greater binding ability of the $\text{SO}_3\text{·NH}_3$ heterodimer with product SFA than with reactant NH_3 . Finally, the complex C3 proceeds via transition state TS3 to form a hydrogen-bonding complex P3. In the mechanism above, the product

Table 1. Calculated Forward/Reverse Rate Coefficients (k_7/k_{-7} and k_8/k_{-8}), the Unimolecular Rate Constant (k_9), the Concentration of Catalyst ($[M]$), and the Reaction Rate Constant (k) for the Reaction of $\text{SO}_3 + \text{NH}_3$ without a Catalyst, with Reactant NH_3 as a Self-catalyst, and the Product SFA as an Autocatalyst

| | without catalyst | NH_3 self-catalysis | SFA autocatalysis (under laboratory conditions) | SFA autocatalysis (under atmospheric conditions) |
|--|------------------------|--|--|--|
| k_7 ($\text{cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$) | 4.35×10^{-10} | 4.35×10^{-10} | 4.35×10^{-10} | 4.35×10^{-10} |
| k_{-7} (s^{-1}) | 5.32×10^2 | 5.32×10^2 | 5.32×10^2 | 5.32×10^2 |
| k_8 ($\text{cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$) | | 4.96×10^{-10} | 3.96×10^{-10} | 3.96×10^{-10} |
| k_{-8} (s^{-1}) | | 1.99×10^8 | 4.12×10^2 | 4.12×10^2 |
| k_9 (s^{-1}) | 1.64×10^{-8} | 4.46×10^8 | 1.53×10^6 | 1.53×10^6 |
| $[M]$ (molecules cm^{-3}) | | 10^9 – 10^{13} | 10^{11} – 10^{15} | 10^4 – 10^8 |
| k ($\text{cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$) | 1.33×10^{-20} | 2.78×10^{-13} to 2.72×10^{-10} | 3.01×10^{-11} to 4.34×10^{-10} | 3.23×10^{-18} to 4.34×10^{-14} |
| effective rate constant ^{28,29} | | 10^{-12} – 10^{-10} ($\text{cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$) (laboratory conditions) | | |

SFA molecule, as an autocatalyst, mediates the formation of the N–S covalent bond by transfer of a proton from NH_3 to an oxygen atom of SO_3 . These computations indicate that either the reactant or product can function as a catalyst to make the reaction between SO_3 with NH_3 much more energetically accessible, as observed in previous experiments.

Reaction Rate of the SO_3 – NH_3 Reaction. Given the self-catalysis ability of reactant NH_3 and the autocatalysis ability of product SFA, it is important to examine the reaction rate of the SO_3 and NH_3 reaction and compare this rate with that of the SO_3 and H_2O reaction to determine if the reaction with NH_3 is an important loss pathway for SO_3 . Kinetic calculations are carried out based on conventional transition-state theory (TST)^{24,25,76–78} to evaluate the effects of NH_3 and SFA on the rate constants for the reaction between SO_3 and NH_3 . Besides, the TST with Wigner tunneling correction is also considered (see Table S3), and the results indicate that the tunneling effect has little impact on the reaction rate constant. As previously described, the self- or autocatalyzed reaction mainly proceeds via the following reaction sequence:



where M represents the catalyst (reactant NH_3 or product SFA). The energy profiles for reaction steps 7–10 shown in Figure 1b,c indicate that reaction 9 is the rate-determining step. Applying the steady-state approximation to the prereactive complex and assuming that the complex is in equilibrium with the reactant, we derive the following equation:

$$\begin{aligned} r &= \frac{d[\text{SFA}]}{dt} \\ &= \frac{k_7}{(k_{-7} + k_8[\text{M}])} \times \frac{k_8}{(k_{-8} + k_9)} \times k_{10}[\text{SO}_3][\text{NH}_3][\text{M}] \end{aligned} \quad (11)$$

where k_7/k_{-7} and k_8/k_{-8} denote the ratio of the forward/reverse rate coefficients for reactions 7 and 8, respectively, and k_9 is the unimolecular rate constant for reaction 9. Thus, the rate constant k for reaction 2 can be expressed as

$$k = \frac{r}{[\text{SO}_3][\text{NH}_3]} = \frac{k_7}{(k_{-7} + k_8[\text{M}])} \times \frac{k_8}{(k_{-8} + k_9)} \times k_{10}[\text{M}] \quad (12)$$

where k can be viewed as a measure of the relative efficiency of different catalysts because their concentrations are also included in eq 12.

For SFA, wide concentration ranges from 10^{11} to 10^{15} molecules cm^{-3} and from 10^4 to 10^8 molecules cm^{-3} are examined, respectively, reflecting an SO_3 concentration of 10^9 – 10^{13} molecules cm^{-3} examined in the laboratory, and a concentration of 10^0 – 10^5 molecules cm^{-3} observed in the atmosphere (see Tables S4 and S5). The computed rate constants for both conditions are presented in Table 1. Without considering the catalyst, the rate constant k is $\sim 10^{-20}$ $\text{cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$, which is too small for the reaction to occur. Under typical laboratory conditions, the reaction rate constant k for the SO_3 and NH_3 reaction catalyzed by either reactant NH_3 or product SFA increases significantly, and the rate constant can be as high as 10^{-10} $\text{cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$, consistent with the experimentally measured value.^{28,29} Both reactant self-catalysis and product autocatalysis mechanisms can explain the observed spectral signals of SFA formed from SO_3 (in the presence of SO_2 and O_2) and NH_3 in the laboratory.³⁰ However, considering that the product SFA concentration is significantly lower than that observed in the experiment (10^4 to 10^8 molecules cm^{-3} in Table S5), the high reaction rate constant (10^{-10} $\text{cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$) would be difficult to attain through SFA autocatalysis alone. Thus, we expect that the reaction through NH_3 self-catalysis is the major sink of SO_3 in areas with abundant NH_3 in the atmosphere.

The competition between the two reactions, one between SO_3 and NH_3 and the other between SO_3 and H_2O , also warrants investigation given that the latter reaction is generally considered as the dominant loss process of SO_3 . The rate constant of the SO_3 and $(\text{H}_2\text{O})_2$ reaction is 10^{-11} – 10^{-10} $\text{cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$ for H_2O -involved self-catalysis reaction.²⁶ Under normal atmospheric conditions, the concentration of $(\text{H}_2\text{O})_2$ ($\sim 10^{14}$ molecules cm^{-3})^{79,80} is much higher than that of NH_3 ; hence, the reaction with H_2O will be the dominant sink pathway for SO_3 . However, in highly polluted areas with relatively dry conditions, the concentration of NH_3 can be comparable with that of $(\text{H}_2\text{O})_2$; thus, the reaction between SO_3 and NH_3 can potentially compete with the reaction between SO_3 and H_2O (ratios of the rates of the two reactions are given in Tables S6–S9). Note also that Bandyopadhyay et

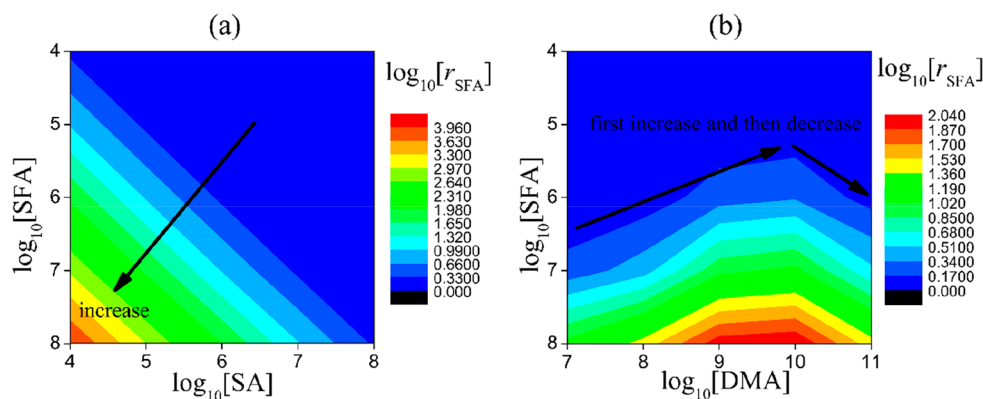


Figure 2. (a) Cluster formation rates ratio (r_{SFA}) versus the logarithm of [SA] and [SFA] at [DMA] = 10^9 molecules cm^{-3} and (b) the logarithm of [DMA] and [SFA] ($T = 278$ K and $10^4 \leq [\text{SFA}] \leq 10^8$ molecules cm^{-3}). The color bars are values for $\log_{10}[r_{\text{SFA}}]$.

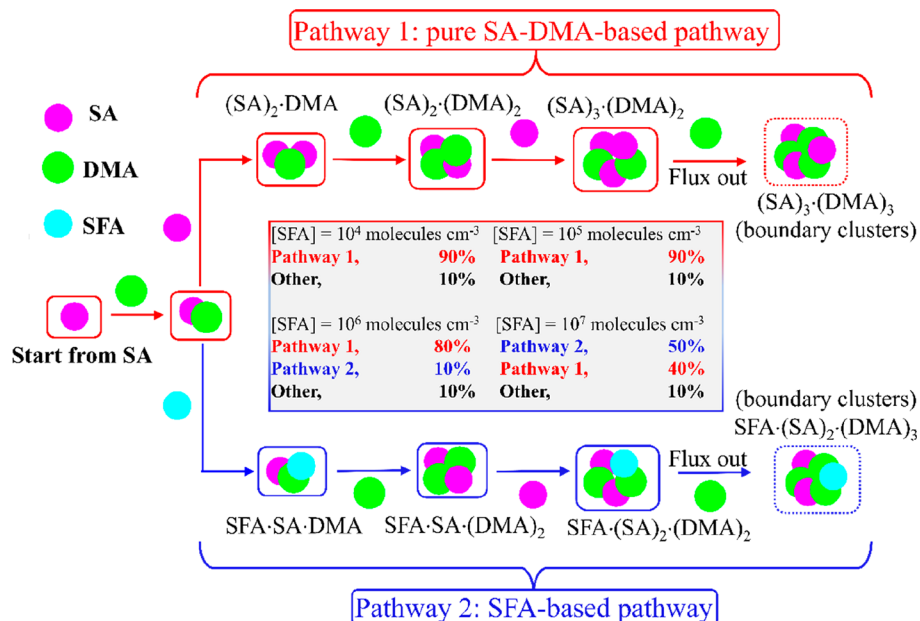


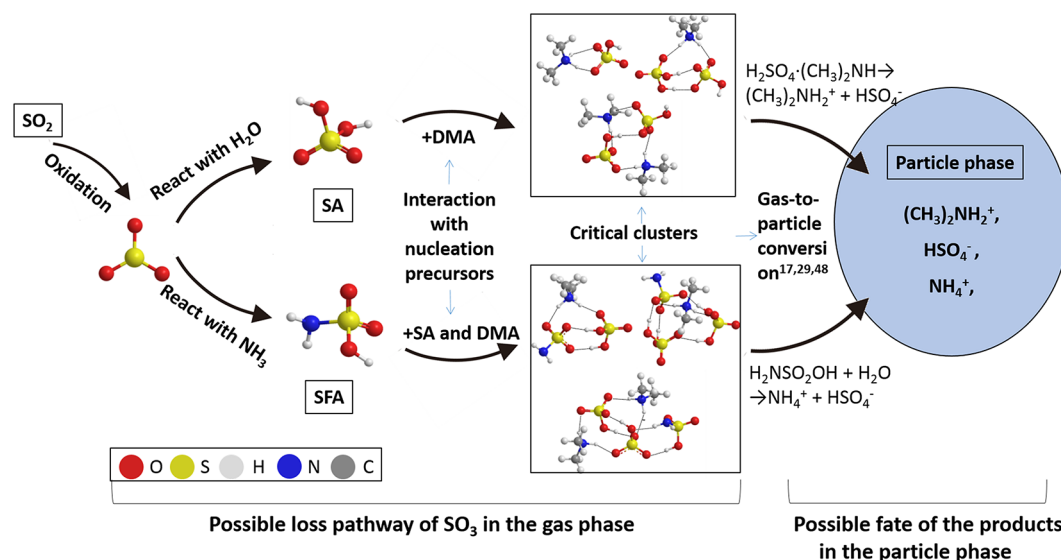
Figure 3. Main pathways and the corresponding mechanism of cluster growth within the cluster size range considered, at $T = 278$ K, $[\text{SA}] = 10^6$ molecules cm^{-3} , $[\text{DMA}] = 10^9$ molecules cm^{-3} , and $10^4 \leq [\text{SFA}] \leq 10^8$ molecules cm^{-3} . The blue and red fluxes represent the growth pathways of SFA-contained clusters and pure SA-DMA-based clusters, respectively.

al.²⁶ suggested that the $\text{SO}_3 + \text{H}_2\text{O}$ reaction could also be effectively catalyzed by NH_3 molecule, with a high reaction rate constant ($\sim 10^{-4}$ cm^3 molecule $^{-1}$ s $^{-1}$) for SO_3 and $\text{H}_2\text{O}\cdot\text{NH}_3$ reaction. Given that the $\text{H}_2\text{O}\cdot\text{NH}_3$ concentration is several orders of magnitude lower than that of $(\text{H}_2\text{O})_2$ or NH_3 , the reaction of SO_3 and NH_3 could also be competitive with that of SO_3 and $\text{H}_2\text{O}\cdot\text{NH}_3$ (ratios of the rates of the two reactions are given in Tables S10–S12).

Atmospheric Implication: Enhancement Effect of SFA on NPF. Knowing that the formation of SFA becomes an important and competitive loss pathway for SO_3 in the atmosphere with a high concentration of NH_3 , we performed ACDC simulations to achieve a deeper understanding of the influence of SFA on SA-DMA-based molecular clustering, a known source for NPF.⁴⁸ The ratio (r_{SFA}) of formation rates with SFA to the rate without SFA is given by eq 13 for temperature $T = 298, 278,$ and 258 K, corresponding to the temperature conditions in the boundary layer and in the lower troposphere:⁸¹

$$r_{\text{SFA}} = \frac{J([\text{SFA}] = x, [\text{SA}] = y, [\text{DMA}] = z)}{J([\text{SA}] = y, [\text{DMA}] = z)} \quad (13)$$

where [SFA], [SA], and [DMA] stand for SFA, SA, and DMA concentrations, respectively. [SFA] was varied from 10^4 to 10^8 molecules cm^{-3} (Table S5); the 10^4 – 10^8 molecules cm^{-3} of [SA] and 10^7 – 10^{11} molecules cm^{-3} of [DMA] are chosen since these values are the typical observed values in the atmosphere.^{82–84} The enhancement factor (r_{SFA}) at three different temperatures (Tables S14–S16, Figures S1–S2; Figure 2) is always equal to or larger than 1.0, reflecting the enhancement ability of SFA on the SA-DMA-based system. At 278 K, for example, the dependence of the enhancement factor r_{SFA} on [SFA], [SA], and [DMA] is shown in Figure 2. The r_{SFA} increases with increasing [SFA] and reaches as high as 10^5 at $[\text{SFA}] = 10^8$ molecules cm^{-3} (Figure 2a,b) with low [SA] of 10^4 molecules cm^{-3} . Generally, high absolute cluster formation rates relevant to observed atmospheric NPF^{46,50,84,85} are associated with fairly low values of r_{SFA} (Tables S14–S16). However, the enhancement effect of SFA may still be

Scheme 1. Suggested Scheme of the Important Loss Pathway for SO₃ in Highly Polluted Atmosphere with a High NH₃ Concentration

significant in many atmospherically relevant conditions; for example at $[SA] = 10^6$ and $[DMA] = 10^{10}$ molecules cm^{-3} , an SFA concentration of 10^6 leads to an enhancement factor of 2 at $T = 298$ K and an overall formation rate of $J = 115$ $\text{cm}^{-3} \text{s}^{-1}$.

Moreover, r_{SFA} decreases as $[SA]$ increases, as shown in Figure 2a, likely due to the stronger binding between SA and DMA than between SFA and DMA (or between SFA and SA). At a constant concentration of SFA and DMA, increasing SA leads to increased SA-DMA clustering at the expense of SFA-containing clusters, and also to decreased r_{SFA} , even as the overall particle formation rate increases. The influence of $[DMA]$ on the ratio r_{SFA} shows a different trend compared with that of $[SA]$ (Figure 2b), where r_{SFA} increases first as $[DMA]$ changes from 10^7 to 10^{10} molecules cm^{-3} . This might be due to the increased hydrogen bonding interaction between acidic molecule SFA and the added base molecule DMA. As such, with the increase of $[DMA]$ to 10^9 molecules cm^{-3} , saturation of hydrogen bonding interaction is reached for SFA, thus resulting in the maximum enhancement strength, whereas with further increase of $[DMA]$, r_{SFA} decreases as $[DMA]$ changes from 10^{10} to 10^{11} molecules cm^{-3} . This is because the hydrogen bonds between SFA and SA could be disrupted by the added DMA molecules, leading to the decreased interaction between SFA with other molecules, thereby decreasing the r_{SFA} . This phenomenon could be a common feature for the system involving acidic compounds, such as HMSA and glycolic acid.^{37,86} Furthermore, the variation of enhancement factor with the increase of $[DMA]$ in the presence of NH_3 is further examined (Figure S3). The results show that the enhancement factor of SFA first increases and then decreases with increasing $[DMA]$, while the relatively high $[\text{NH}_3]$ of 10^{10} to 10^{11} molecules cm^{-3} has only a minor effect.

To further identify the mechanism by which SFA offers its enhancement effect, the main pathways of cluster growth were traced using ACDC. The principal growth paths of SFA-SA-DMA-based clusters at different $[SFA]$ with median $[SA]$ of 10^6 molecules cm^{-3} and $[DMA]$ of 10^9 molecules cm^{-3} at 278 K are shown in Figure 3. At $[SFA] = 10^4$ and 10^5 molecules cm^{-3} , SFA molecules do not substantially contribute to the

cluster growth, and the pathway just shows the growth of pure SA-DMA-based clusters. These results are consistent with those in Figure 2a, where SFA also shows little effect on cluster formation rate. When $[SFA]$ is increased to 10^6 molecules cm^{-3} , SFA appears to be responsible for an alternative pathway (marked by blue lines in Figure 3). In this pathway, the initially generated SFA-containing cluster is SFA-SA-DMA, formed by collision of SFA with a pre-existing SA-DMA cluster. Thereafter, the SFA-SA-DMA cluster grows via a base-stabilization mechanism, and each addition of an acid molecule is stabilized by one additional DMA molecule, following the sequence of acid–base pairs: SFA-SA-DMA \rightarrow SFA-SA-(DMA)₂ \rightarrow SFA-(SA)₂-(DMA)₂ \rightarrow flux out. In this case, the contribution of SFA is only 10%, while with the further increase of $[SFA]$, its role becomes even more important. As shown in Figure 3, SFA plays a dominant role, and its contribution is substantially increased from 10% at $[SFA] = 10^6$ molecules cm^{-3} to 50% at $[SFA] = 10^7$ molecules cm^{-3} .

SFA molecule shows an ability to directly participate in the cluster formation, suggesting that SFA can be a “participator” in facilitating NPF. Contrary to other common acid species as reported in our recent works,^{70,87,88} such organic acids, e.g., lactic acid and glyoxylic acid, and inorganic acids, e.g., nitric acid, can only be indirectly involved in the growth pathway, acting as a “transporter” (which initially participates and eventually evaporates). Note that, like SFA, another two species with sulfonic group, namely, methanesulfonic acid (MSA)³⁶ and hydroxymethanesulfonic acid (HMSA),³⁷ are also identified to directly participate in the cluster formation. However, depending on the formation source of these species, the MSA tends to promote NPF mainly on marine areas. Although HMSA is likely to participate in the process of NPF,³⁷ the formation source of HMSA in the gas phase is still an open question, and its atmospheric concentration still needs to be explored to confirm its roles in NPF. Overall, among the three species containing sulfonic groups, the SFA represents the most compelling species toward NPF in highly polluted areas with high NH_3 concentration.

The environmental fate of SFA is likely to hydrolyze to ammonium sulfate in the aqueous phase, as previously

reported.^{10,30,31} Thus, the formation of SFA-containing molecular clusters, followed by reaction with water and hydrolysis to form ammonium sulfate, may constitute an alternate pathway to sulfate production in the particle phase (see Scheme 1). All the suggested mechanisms may also be extended to the other loss paths of SO₃ with other common bases, such as amines, which are also likely to contribute to the atmospheric sink of SO₃, especially in areas with high concentrations of the base gases. Hence, scenarios involving SFA and its analogues should be assessed on their role in atmospheric particle formation.

CONCLUSION

We have investigated the reaction of NH₃ with SO₃ to form SFA and the subsequent effect of SFA on NPF in highly polluted regions with high concentration of NH₃. The important chemistry found in this study is that, with self-catalysis by the reactant NH₃, the activation barrier for the SO₃-NH₃ reaction can be drastically lowered. Hence, at high NH₃ concentration, the effective reaction rate coefficient can reach $\sim 10^{-10}$ cm³ molecule⁻¹ s⁻¹, indicating that the reaction is sufficiently fast to be competitive with the conventional SO₃-H₂O reaction (effective rate constant of 10^{-11} - 10^{-10} cm³ molecule⁻¹ s⁻¹). This newly identified self-catalyzed reaction provides a previously unreported loss pathway of SO₃ at relatively low H₂O concentration and high NH₃ concentration. Our study shows that the product of the self-catalyzed reaction, SFA, can directly participate in the SA-DMA-based cluster formation, thereby substantially enhancing the cluster formation rate. This new stabilization mechanism in acid-base clustering has important implication to the aerosol NPF in highly polluted regions with high concentrations of base species.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/jacs.8b04928.

Formation Gibbs free energies and the sum of evaporation rates of the clusters; imaginary frequencies of the transition states and the Wigner tunneling correction factor of the reactions; possible concentration of SFA in the experiment and in the real atmosphere; ratio of reaction rate for SO₃ + NH₃ reaction and SO₃ + H₂O reaction under different [NH₃] and [H₂O]; formation Gibbs free energies and a sum of evaporation rates of the clusters containing SFA, SA DMA, and NH₃; enhancement strength of SFA; ratio of cluster formation rates as a function of the logarithm of [SA] and [DMA]; optimized geometries of key species involved in particle formation in gas-phase; ratio of cluster formation rates versus the logarithm of [DMA] (PDF)

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Notes

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