

Realistic Equation of State for Neutron Star Mergers

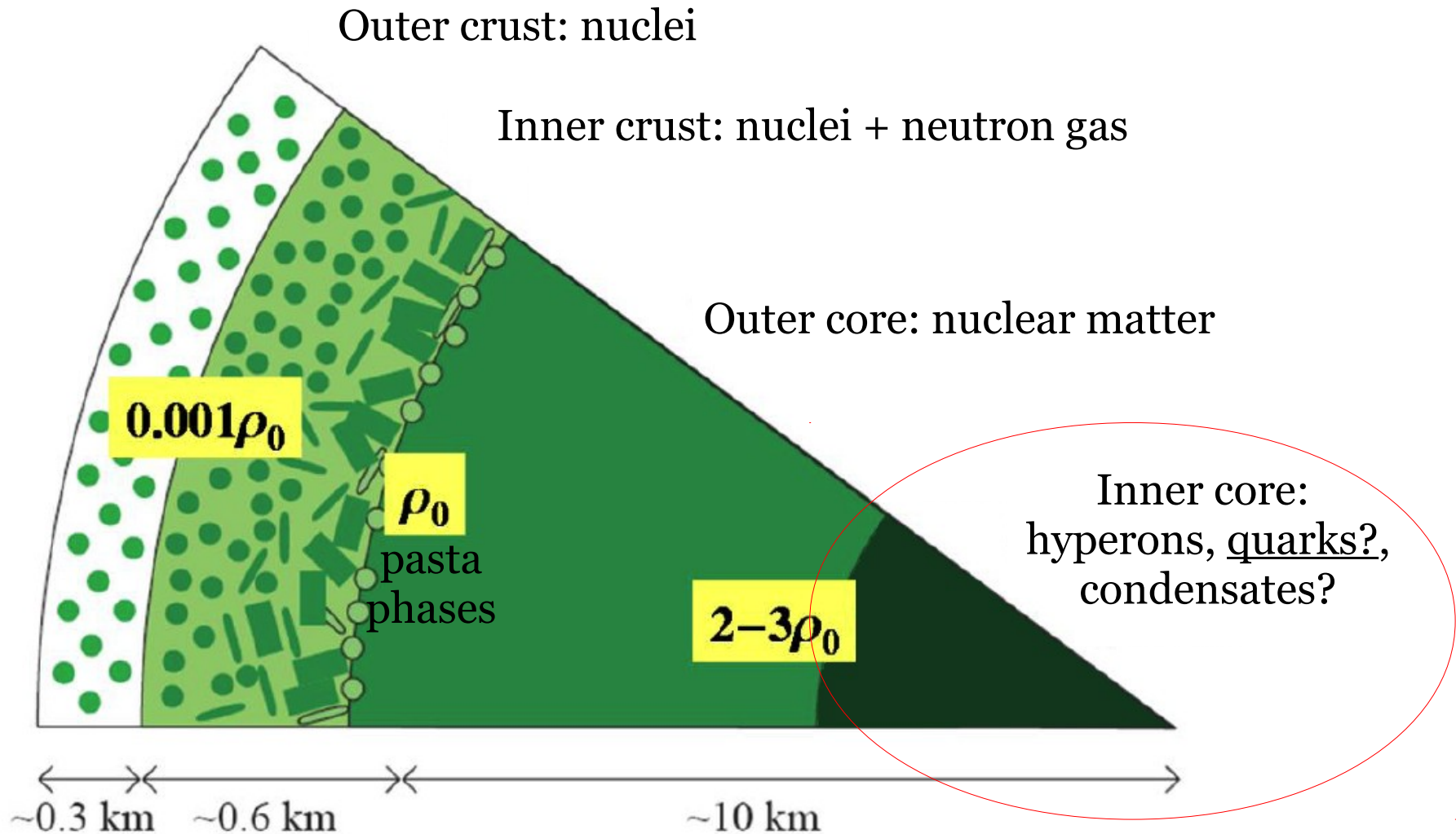


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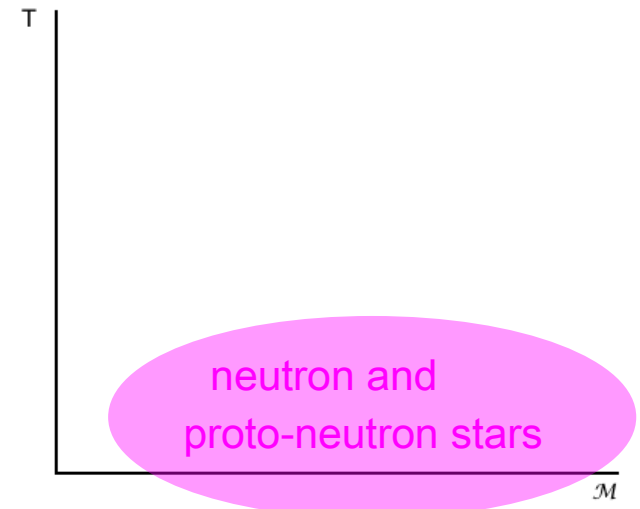
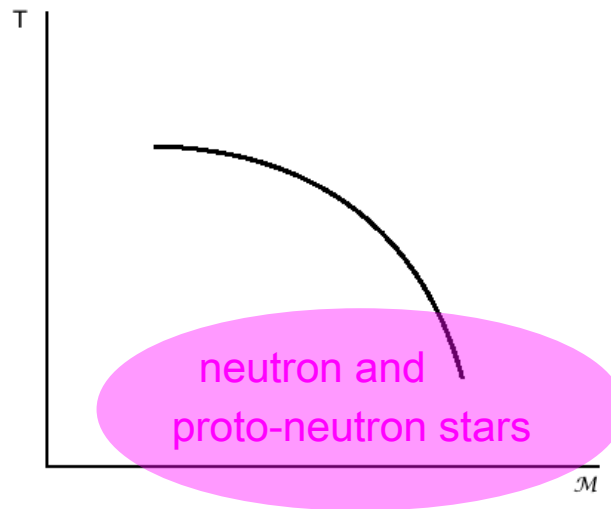
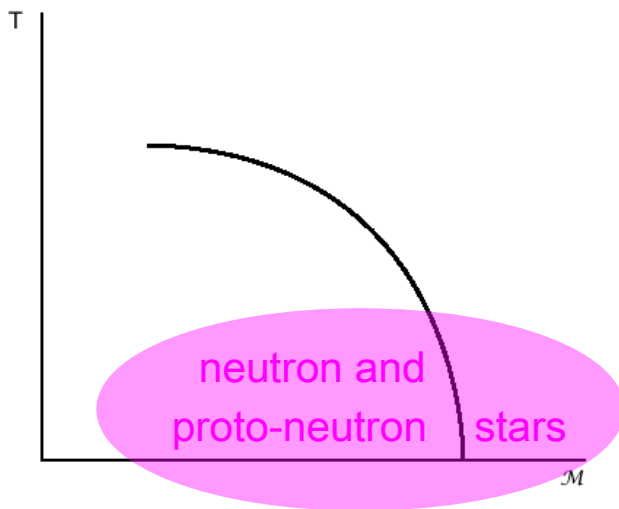
★ Neutron Star Structure:



- nuclear saturation density $\rho_0 \sim 0.15 \text{ fm}^{-3}$ ($0.25 \times 10^{15} \text{ g/cm}^3$)

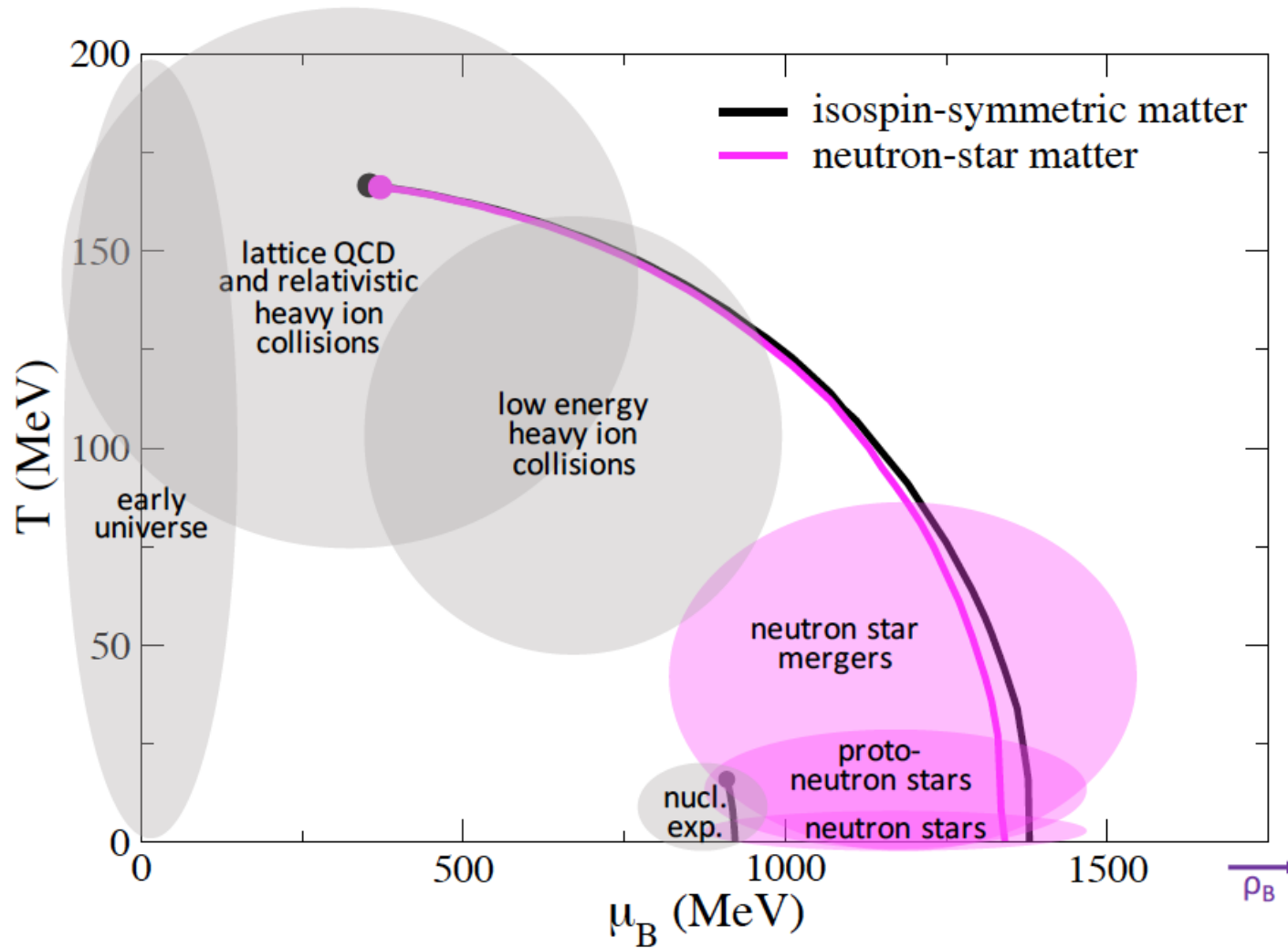
★ QCD Phase Diagram:

- very little information at low temperature
 - strength of transition
 - population



- neutron star mergers?

★ Assuming Continuous Line:



- results from CMF model (no mixtures of phases)

★ CMF (Chiral Mean Field) Model:

- extended non-linear realization of SU(3) sigma model
- uses pseudo-scalar mesons as parameters of chiral transformation
- includes baryon octet (+ leptons) and quarks
- fitted to reproduce nuclear, lattice QCD and astrophysical constraints
- effective masses

$$m_b^* = g_{b\sigma}\sigma + g_{b\delta}\tau_3\delta + g_{b\zeta}\zeta + \delta m_b + g_{b\Phi}\Phi^2$$

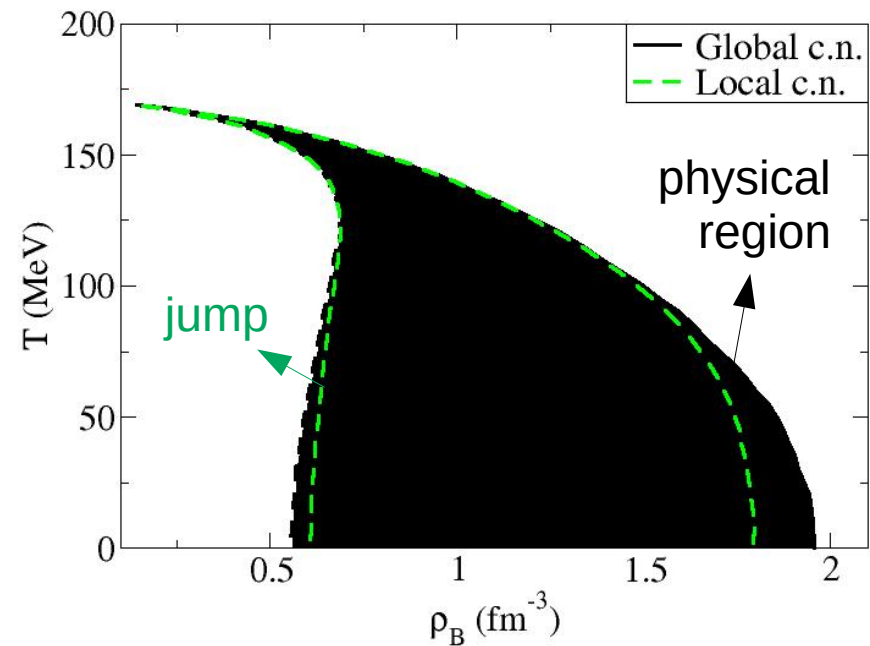
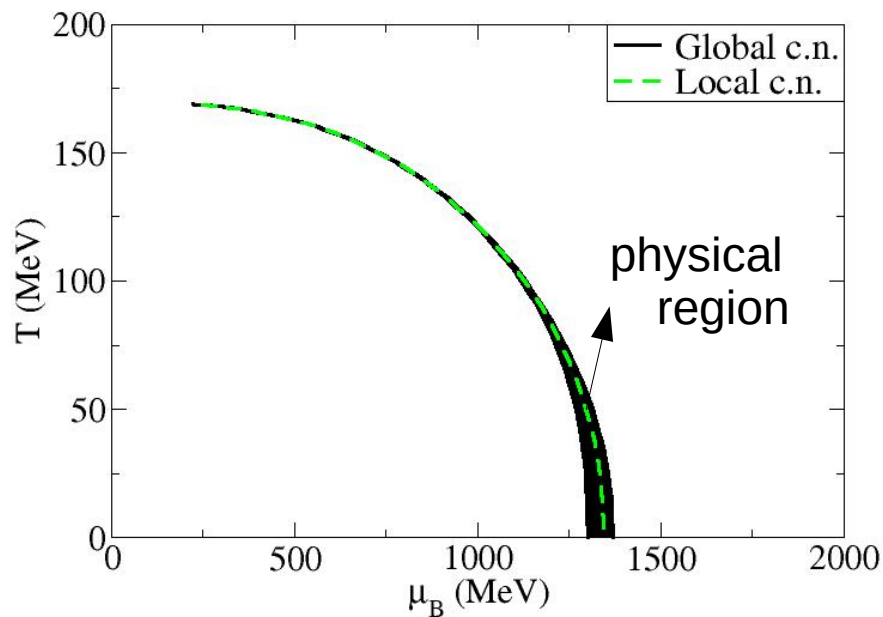
$$m_q^* = g_{q\sigma}\sigma + g_{q\delta}\tau_3\delta + g_{q\zeta}\zeta + \delta m_q + g_{q\Phi}(1 - \Phi)$$

- 1st order phase transitions or crossovers (order parameters σ , Φ)
- potential for Φ (deconfinement)

$$U = (a_0 T^4 + a_1 \mu^4 + a_2 T^2 \mu^2)\phi^2 + a_3 T_0^4 \ln(1 - 6\phi^2 + 8\phi^3 - 3\phi^4)$$

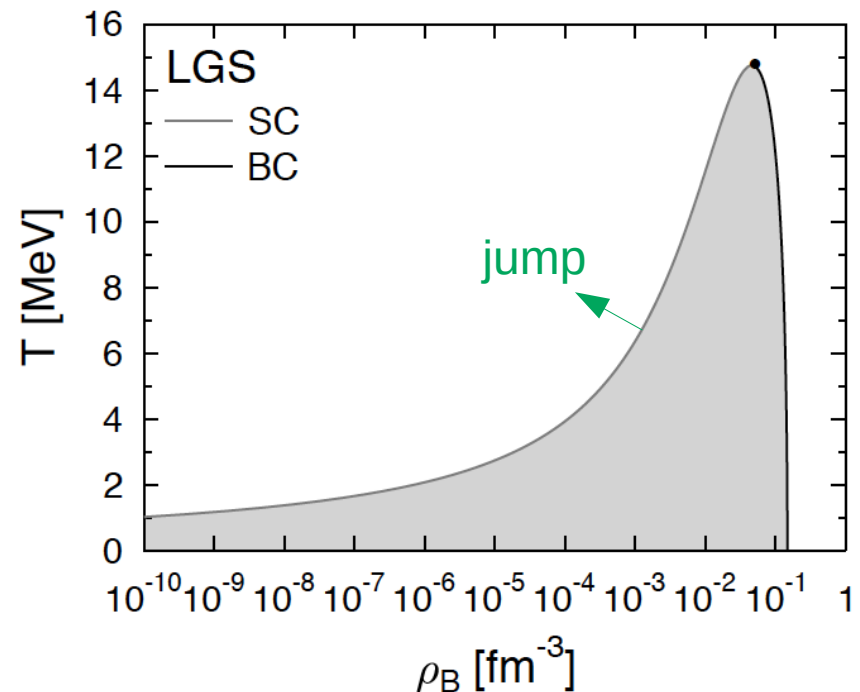
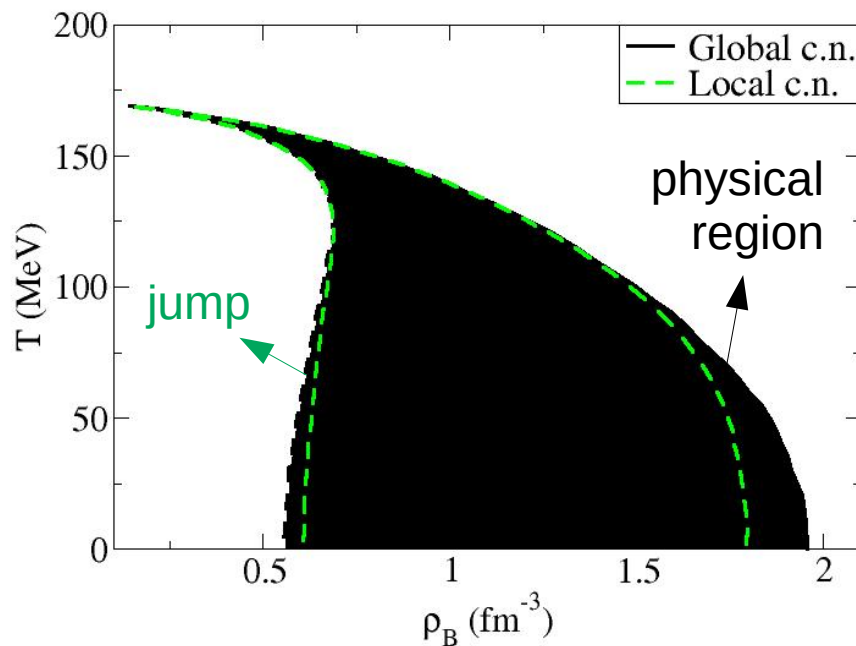
★ Neutron Star Matter: Local vs Global Charge Neutrality:

- absence / presence of mixture of phases: surface tension ???
- “mixed” quantities like $\rho_B = \lambda \rho_B^Q + (1 - \lambda) \rho_B^H$



★ Non-congruent Phase Transitions:

- more than one globally conserved charge within 2 macroscopic phases within a Coulomb-less model: baryon #, electric charge
- local concentration of a charges vary during phase transition
- same chemical potential (assoc. to charge) in both phases (μ_q)
- very different from symmetric matter liquid-gas (LGS)



★ More Comparisons with Nuclear L-G:

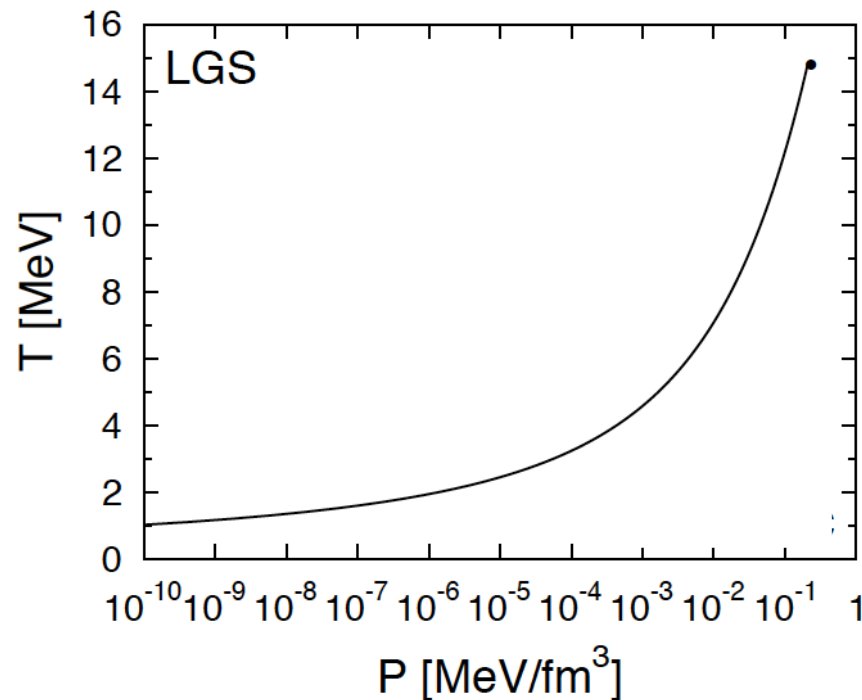
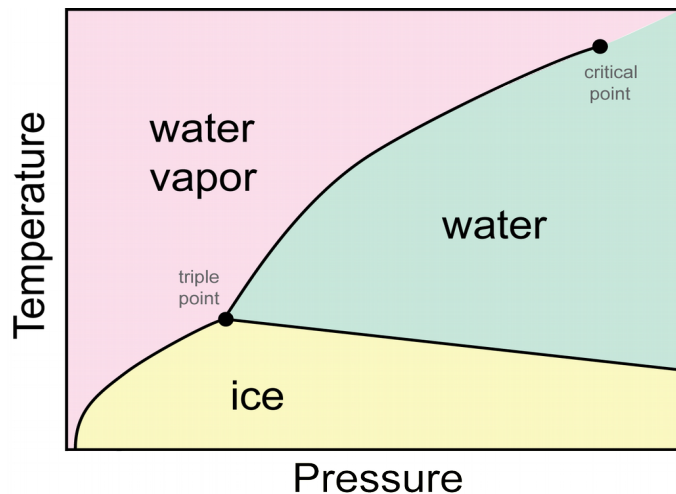
- Clausius-Clapeyron equation
$$\frac{dP}{dT} = \frac{s^I - s^{II}}{1/\rho_B^I - 1/\rho_B^{II}}$$

- $s_q^{II} > s_h^I$, $\rho_{Bq}^{II} > \rho_{Bh}^I$

so $dP/dT < 0$ for deconfinement!

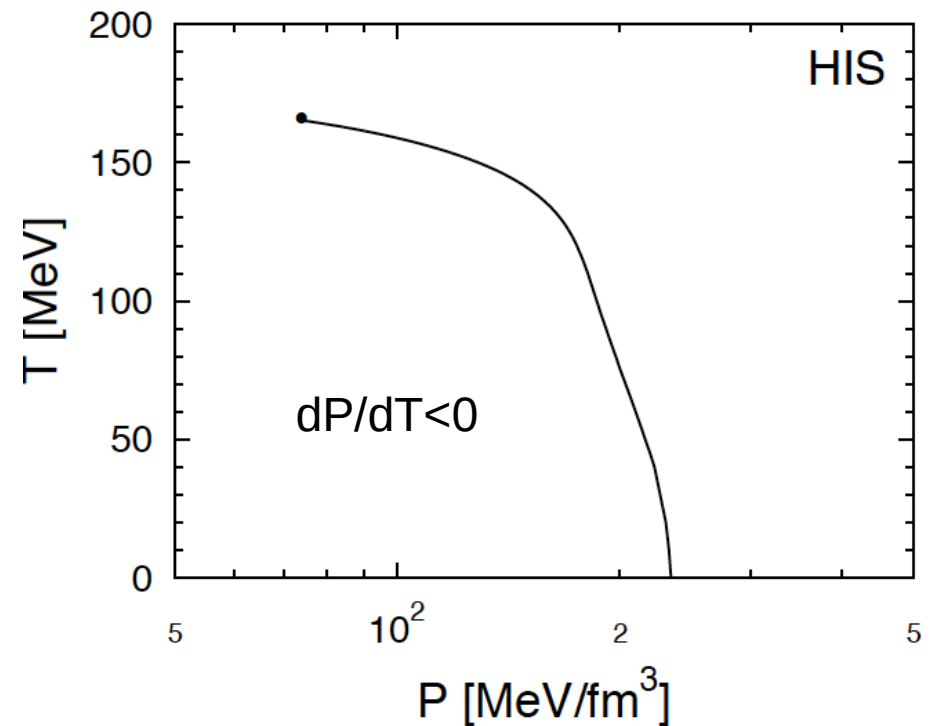
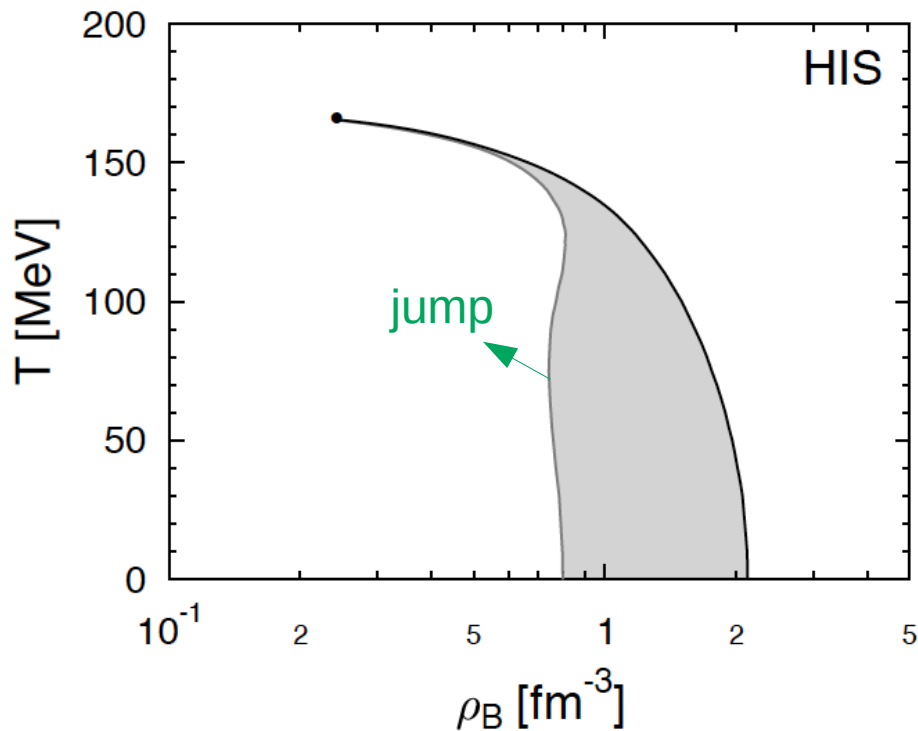
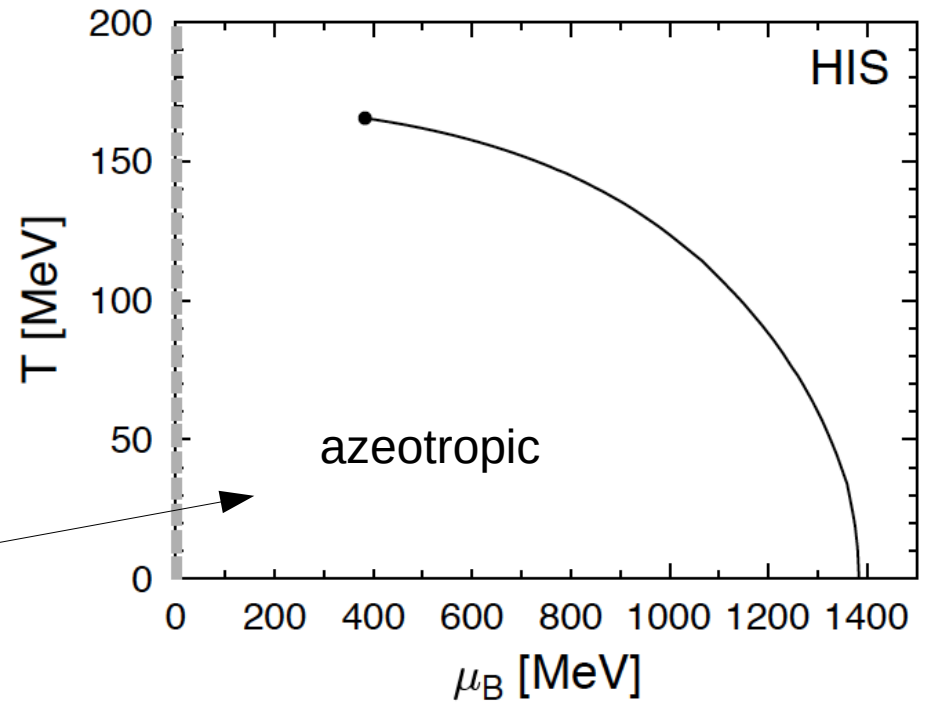
- $s_L^{II} < s_G^I$, $\rho_{BL}^{II} > \rho_{BG}^I$

so $dP/dT > 0$ for LGS



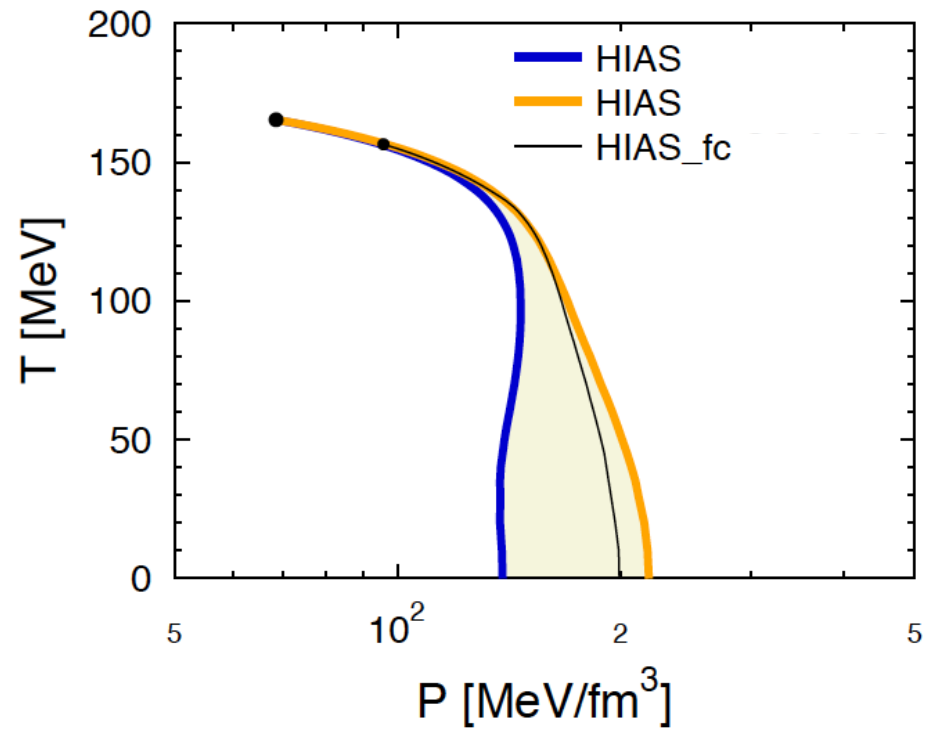
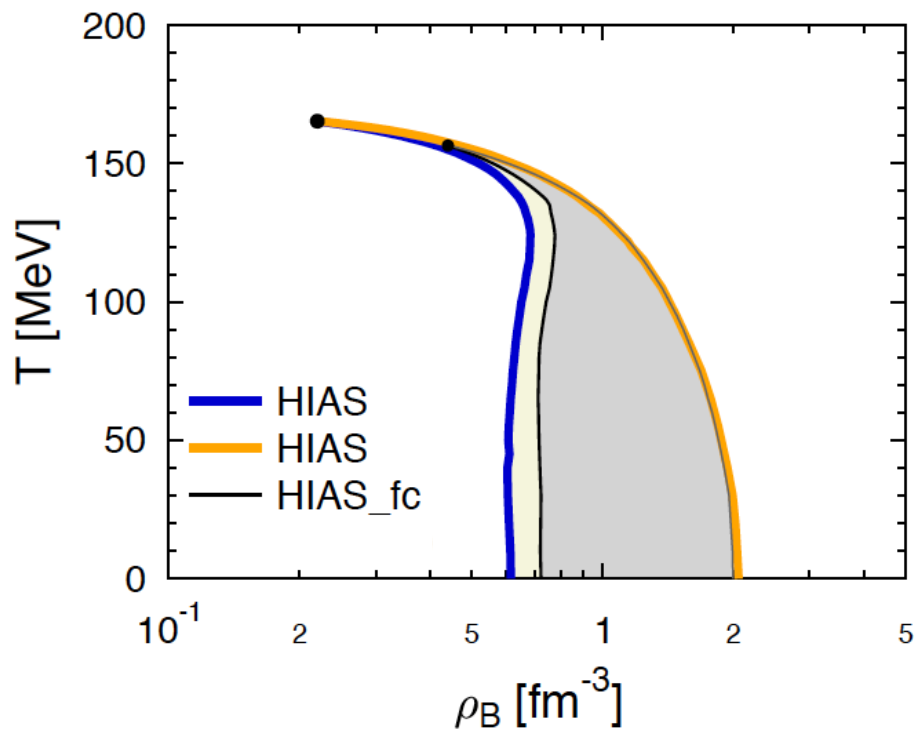
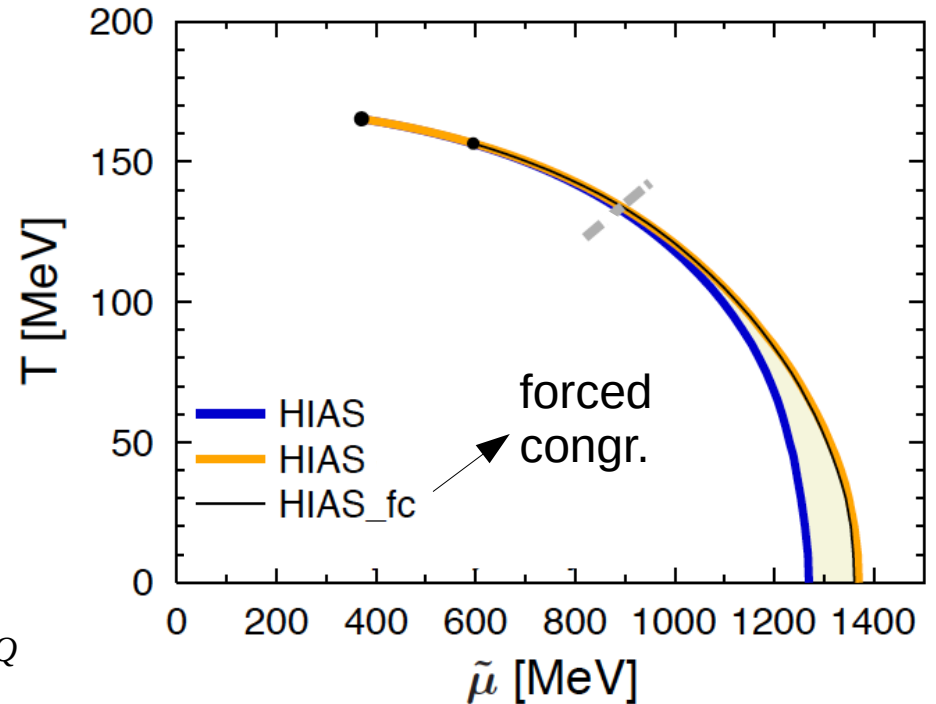
* Symmetric Matter:

- heavy ion collisions
- more than one conserved charge (baryon #, isospin) but a congruent phase transition! ($\mu_q=0$)



* Asymmetric Matter:

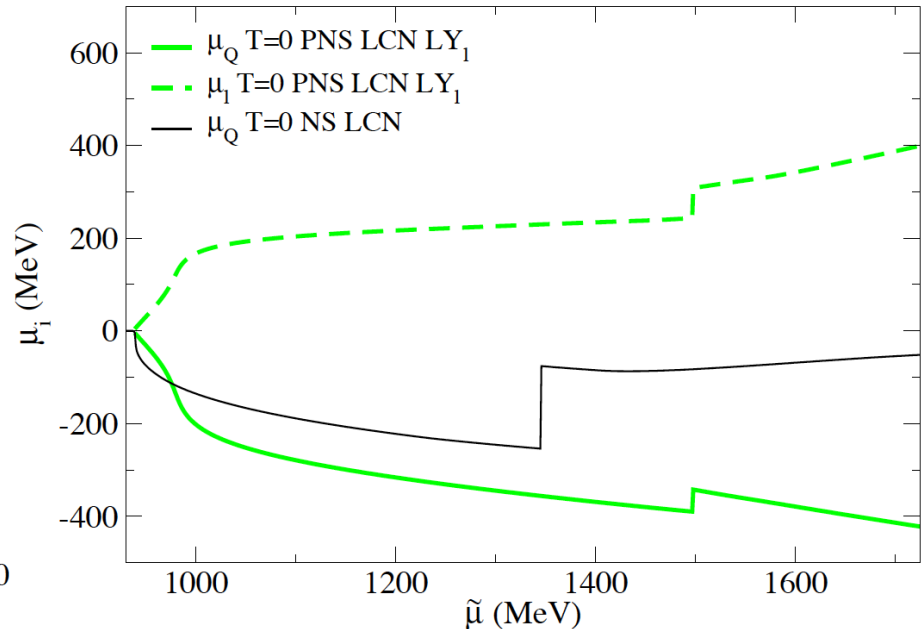
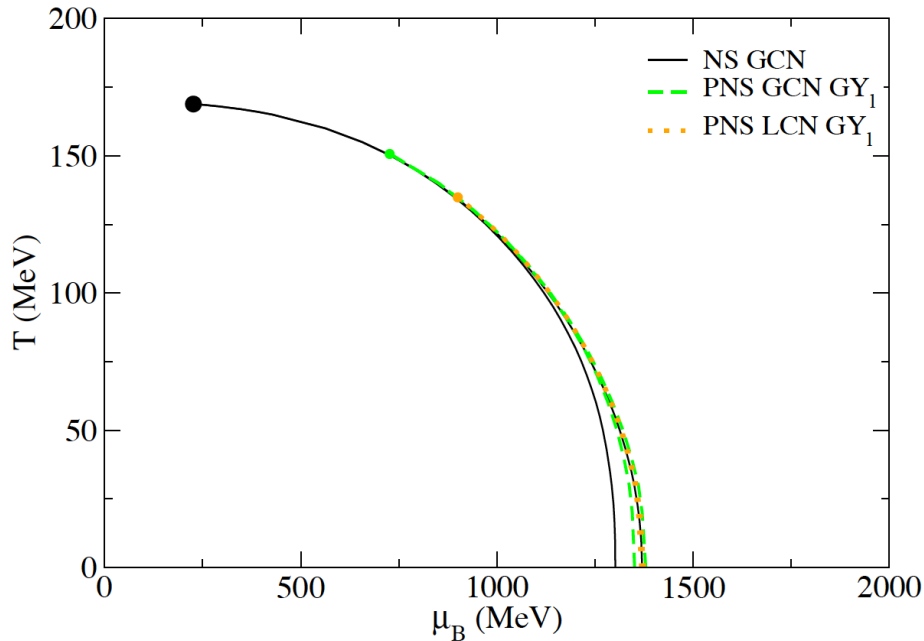
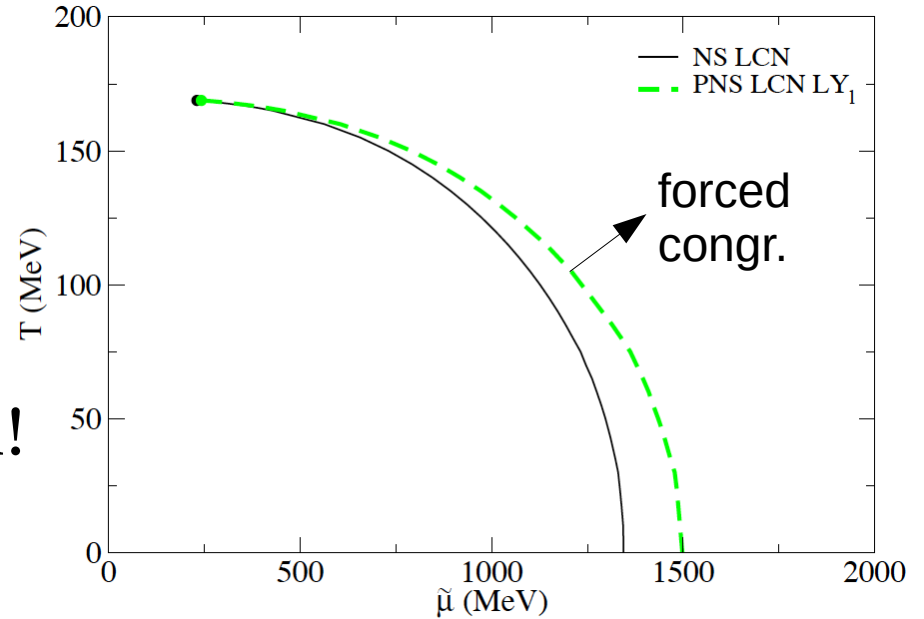
- heavy ion collisions with $Y_Q=0.3$
- more than one conserved charge (baryon #, charge fraction): non-congruent phase transition! $\tilde{\mu} = \mu_B + Y_Q \mu_Q$



★ Proto-Neutron-Star Matter:

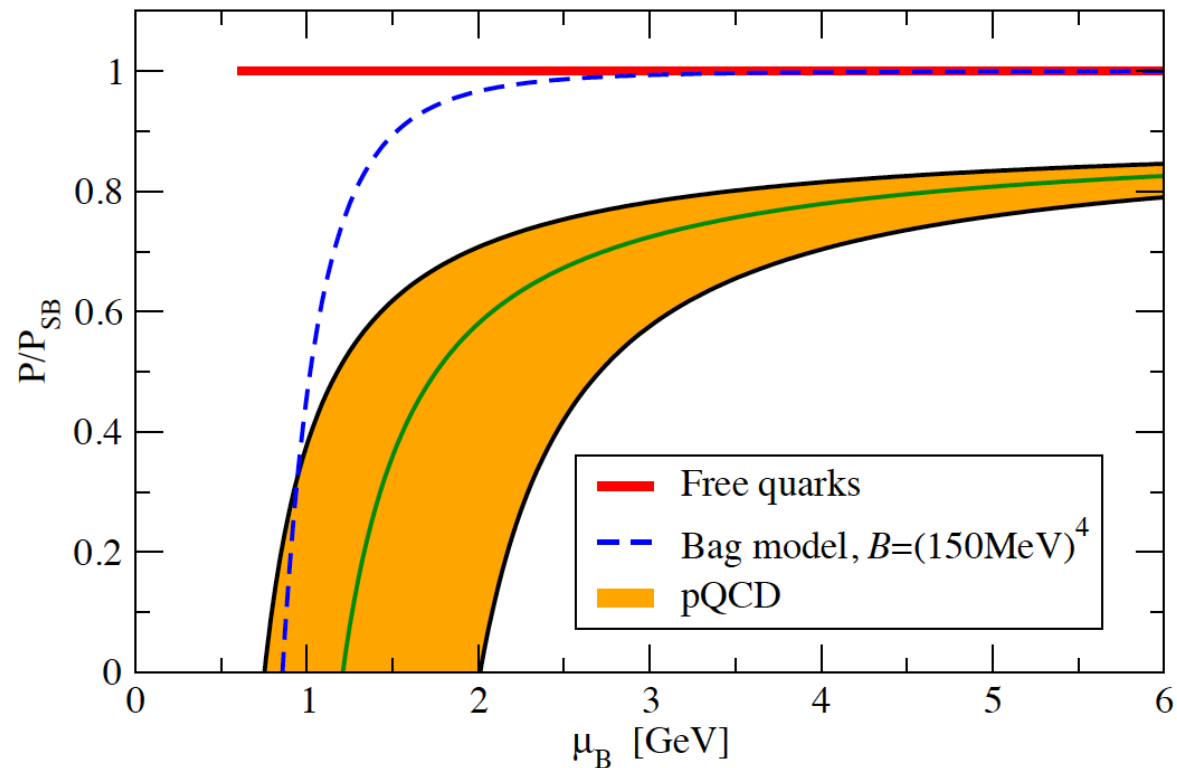
- charge neutral with $Y_1=0.4$
- more than one conserved charge (baryon #, electric charge, lepton fraction):
non-congruent phase transition!

$$\tilde{\mu} = \mu_B + Y_1 \mu_1$$



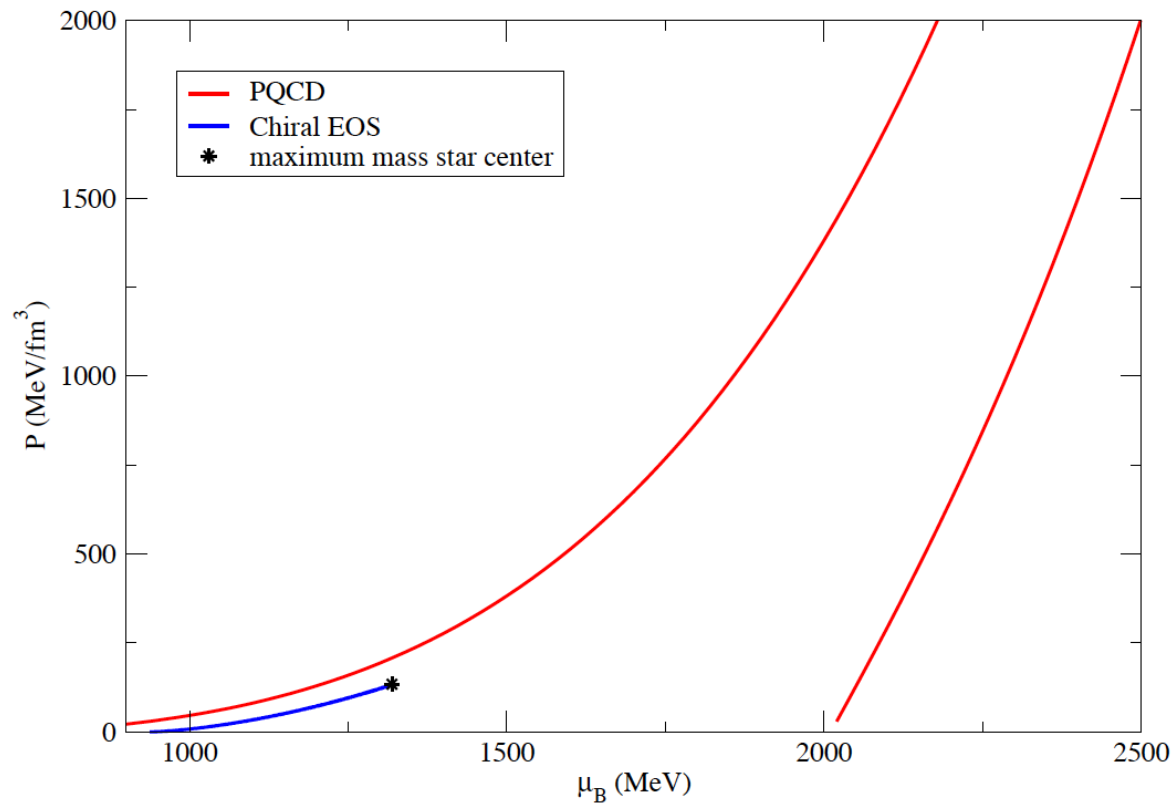
★ Perturbative QCD:

- figure from: Fraga, Kurkela and Vuorinen, *Astrophys. J.* 2014
- 3-flavor QGP at zero temperature including β -equilibrium and charge neutrality
- Bag model failure !



☆ Perturbative limit at T=0

- Chiral EoS until central density of most massive star ($\sim 2 M_{\text{Sun}}$)
- no vector interactions for quarks



★ Perturbative limit at finite temperature

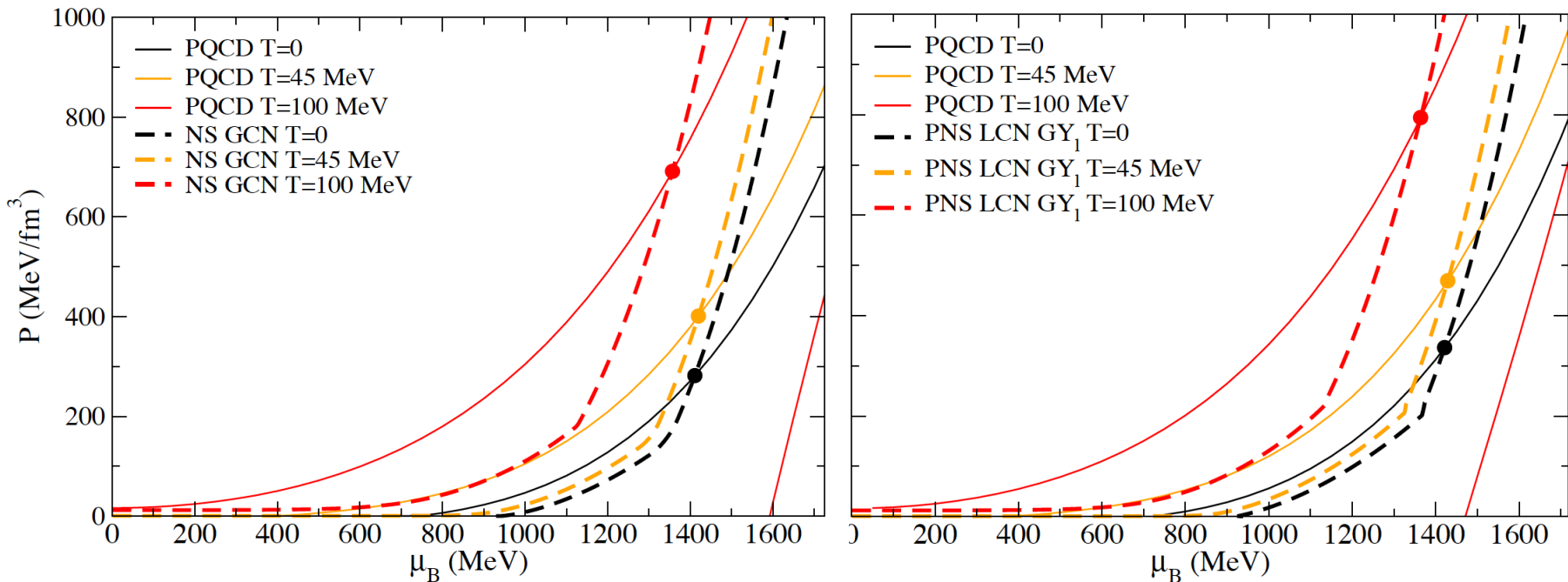
- Chiral EoS limits from PQCD

NS

| | |
|------------------------|-------------------------------|
| $T = 0:$ | $\mu_B = 1411.04 \text{ MeV}$ |
| $T = 45 \text{ MeV}:$ | $\mu_B = 1419.76 \text{ MeV}$ |
| $T = 100 \text{ MeV}:$ | $\mu_B = 1356.87 \text{ MeV}$ |

PNS

| | |
|------------------------|-------------------------------|
| $T = 0:$ | $\mu_B = 1421.69 \text{ MeV}$ |
| $T = 45 \text{ MeV}:$ | $\mu_B = 1429.09 \text{ MeV}$ |
| $T = 100 \text{ MeV}:$ | $\mu_B = 1364.08 \text{ MeV}$ |



★ Conclusions and Outlook

- more investigation of high density part of phase diagram is required!
Signature for 1st order phase transition from astrophysics?
- better understanding of congruent/non-congruent deconfinement phase transitions: finite temperature description, unified EOS (used for L-G transitions) and that provides particle population
- we already have a 3D star merger hadronic EoS table available online at CompOSE (Publ. Astron. Soc. Aust. 34 (2017) e066)
- we are testing the effects of quarks on star mergers using a 3D table
- we are about to include magnetic field and quark pairing effects